

# Bacterial chemotaxis in nutrient replete environments

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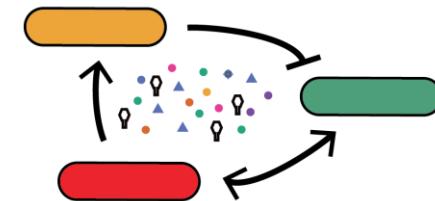
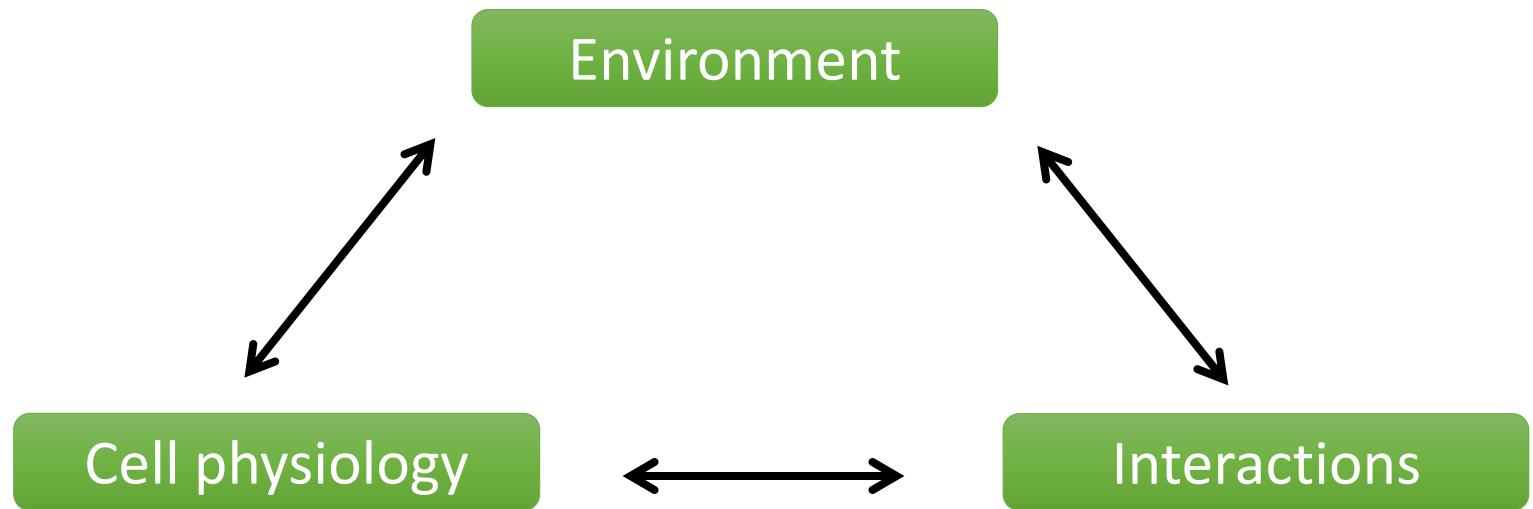
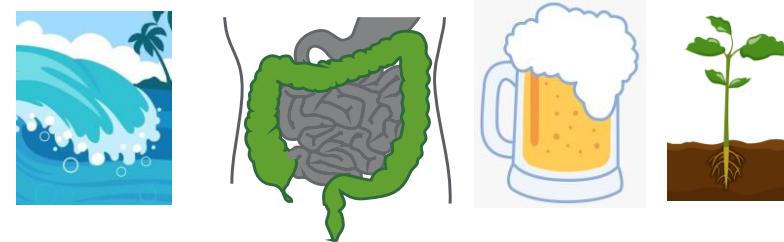
From Jan 2020 in Stanford

Physics LMU Munich

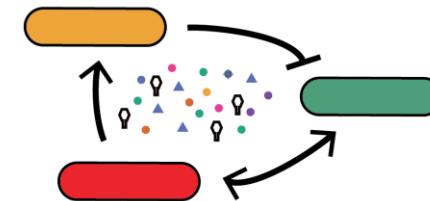
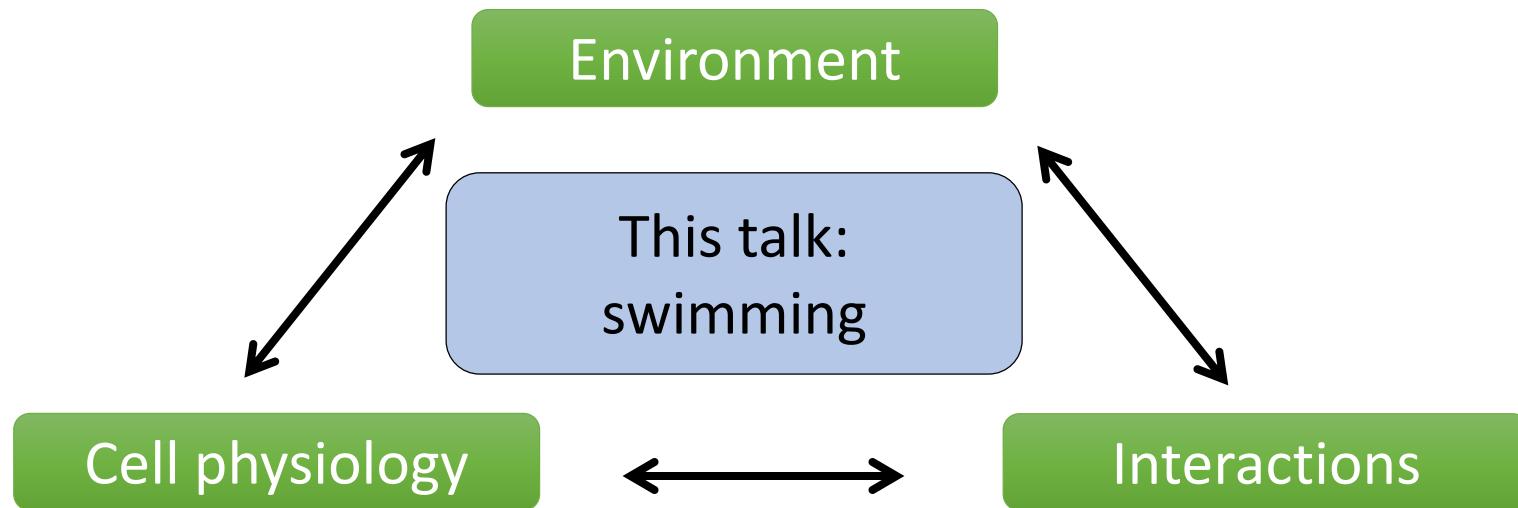
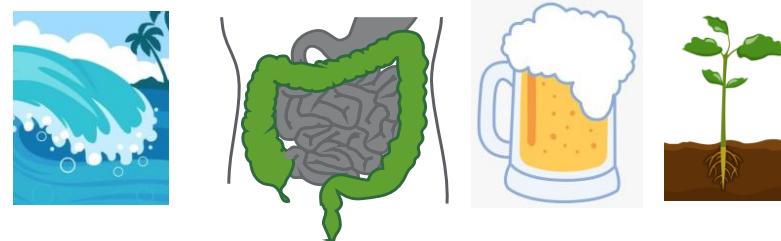
November 2019

[www.bacterialphysiology.com](http://www.bacterialphysiology.com)  
Postdoc positions available!

# Microbes and their communities



# Microbes and their communities



# Acknowledgements

## Chemotaxis



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UCSD



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(Basel)

Urs Jenal (Basel)



**BILL & MELINDA GATES foundation**



# Bacterial chemotaxis: sensing and movement along gradients

Bacteria swim

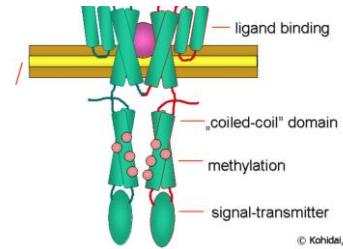


Propulsion by flagella-rotation

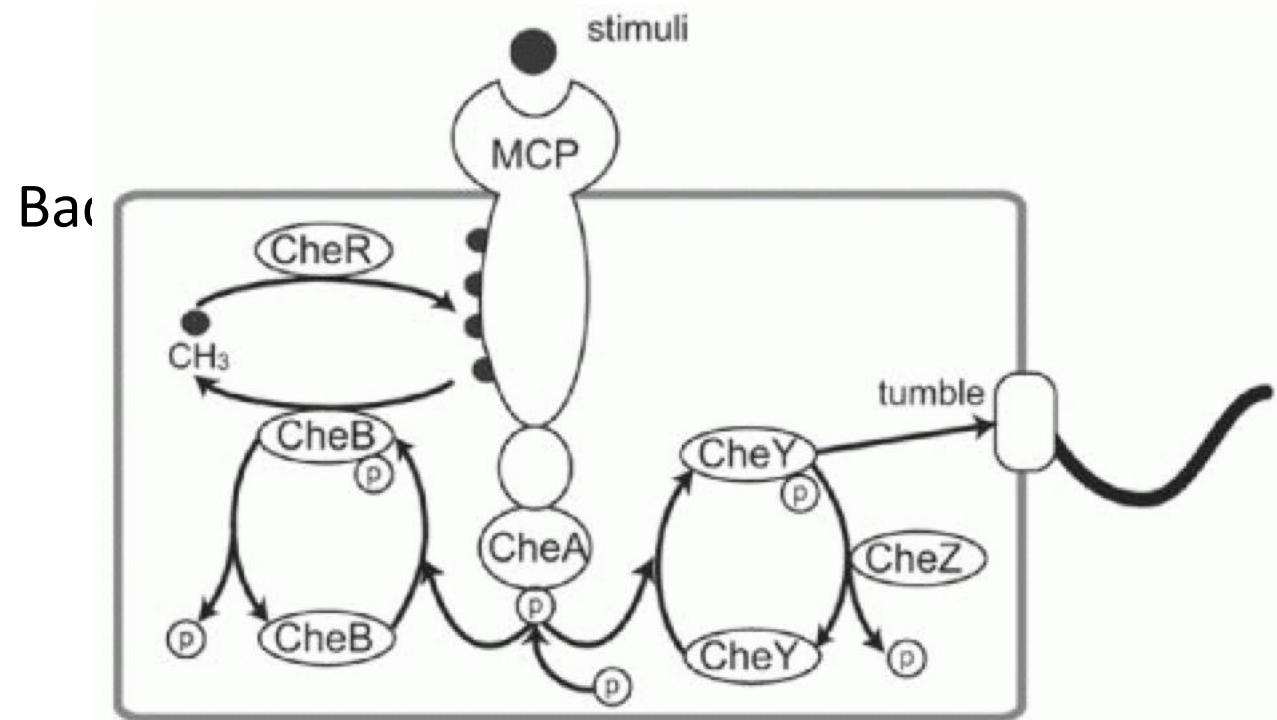
Bacteria sense

For E.coli:

- amino acids
- oxygen
- carbohydrates
- ...



aspartate receptor



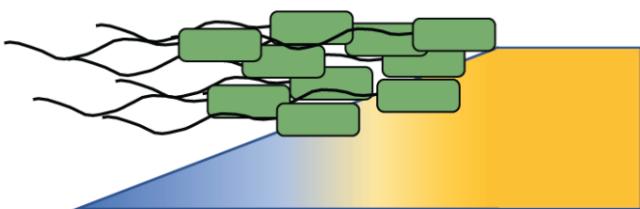
Chemotaxis

What is the physiological role? Advantage of chemotaxis for bacterial cells and populations?

# Chemotaxis is occurring on the population level

Environment sets gradients

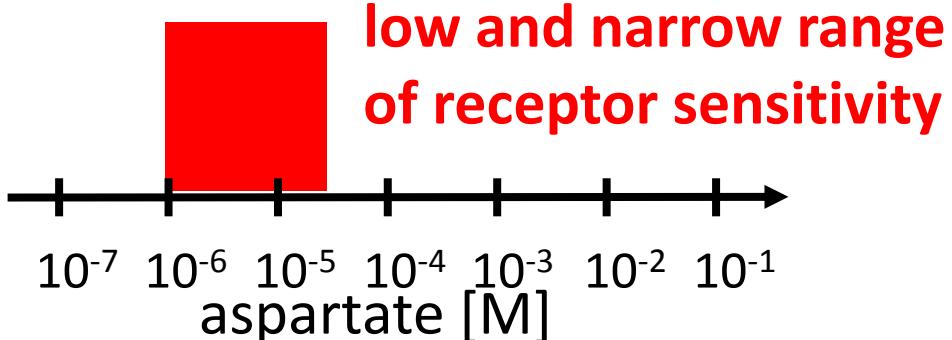
Population sets gradients



consumption  
leads to gradients

attractants (AA, sugars, oxygen) are consumed

Consider aspartate:



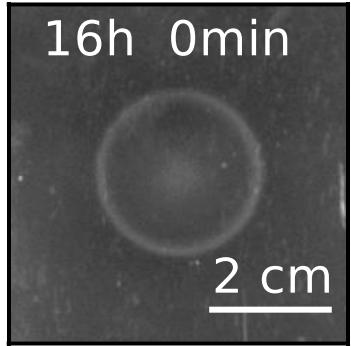
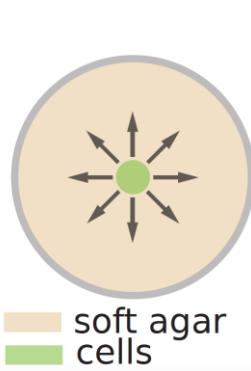
+

high uptake rate  
1/1000<sup>th</sup> of volume occupied by bacteria  
(OD 1): Detectable range consumed  
within ~second

→ Bacteria shape the gradients they sense

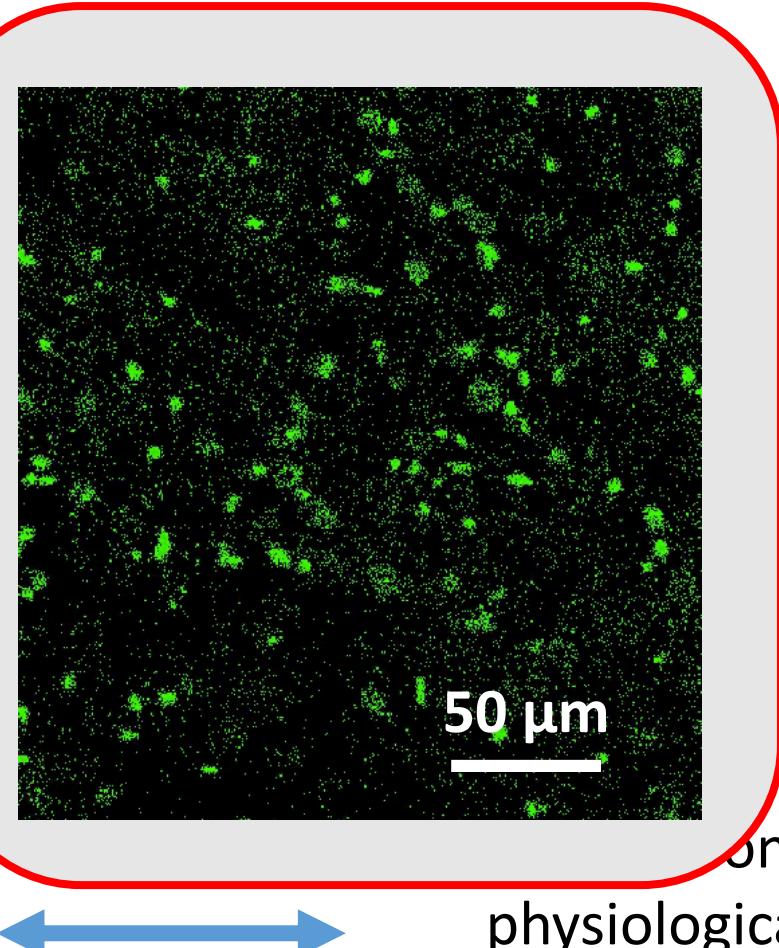
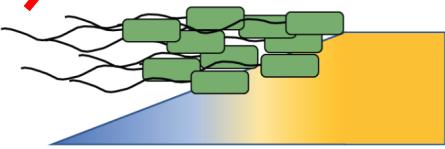
# Colony expansion of chemotactic bacteria

observation in soft-agar: “ring-assay”



E.Coli K-12; growth condition: glycerol +

Chemotaxis  
along gradients



conditions /  
physiological state of cells

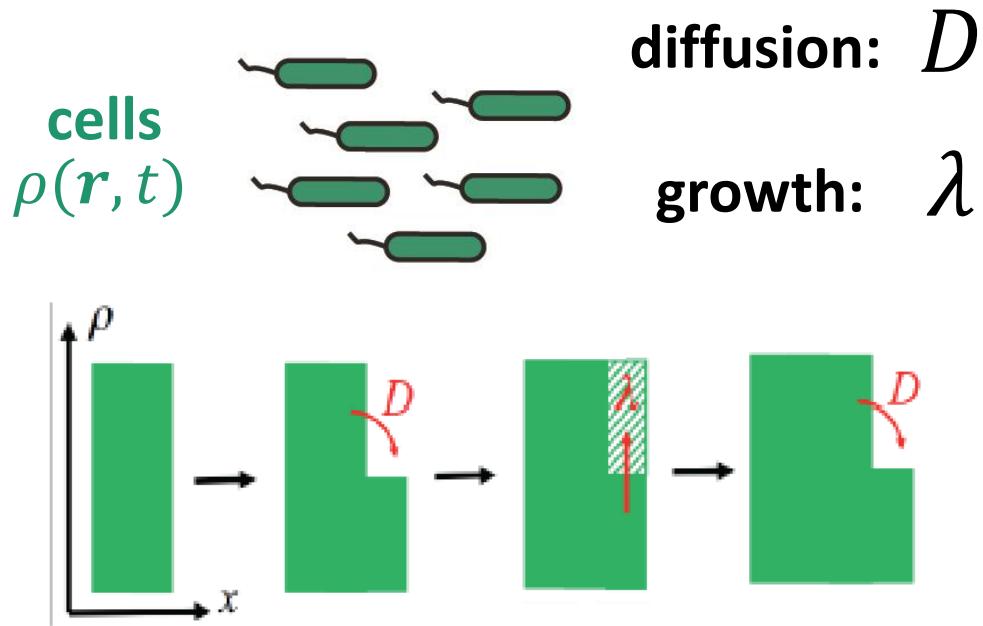
Many experimental and theoretical studies

- [Keller & Segel, 1971][Lauffenburger, 1984][Jiang et al 2010]
- [Saragosti et al, 2011] [Koster et al 2012 ] [Waite et al 2016][Baym et al 2016][Yi & Dean, 2016][Fraebell et al. 2017]
- [Brenner et al, 1998][Saragosti et al, 2010]

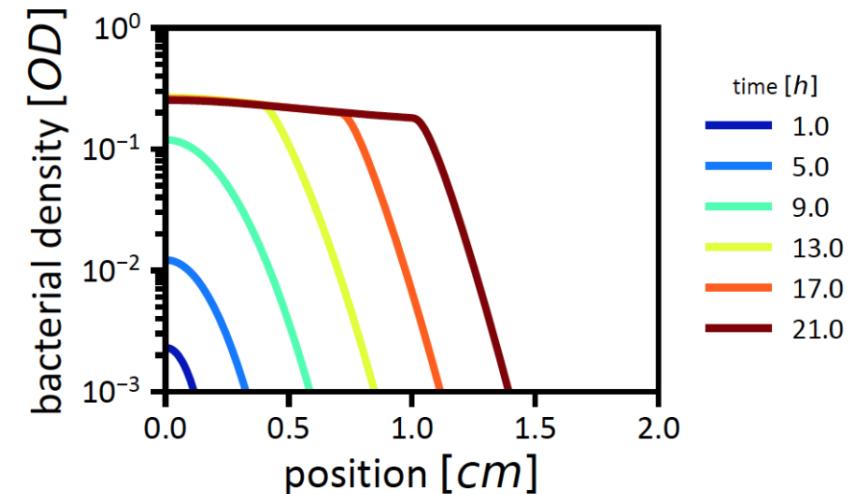
Let's understand a simpler scenario first:  
population expansion without chemotaxis

# Modeling expansion without chemotaxis

- No attractant: undirected run and tumbling
- Cell growth



Model predictions:



expansion speed:  $u_{FK} = 2\sqrt{D \cdot \lambda}$

Fisher-Kolmogorov dynamics

$$\partial_t \rho = D \Delta \rho + \lambda \rho (\rho_{max} - \rho)$$

[Fisher 1937, Kolmogorov et al, 1937]

[Andow et al, 1990, Hallatschek et al, 2007, Korolev et al 2012, Gandhi et al 2016] and others

slope expansion front:  $k = \sqrt{\frac{D}{\lambda}}$

# Can we confirm Fisher-Kolmogorov dynamics for swimming bacteria?

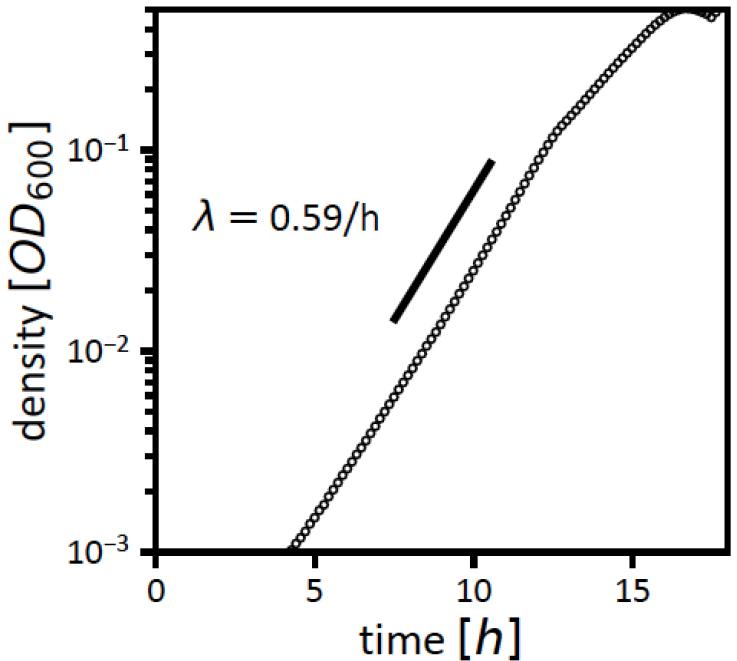
Experimentally: growth in glycerol (not an attractant)

Need to measure cellular diffusion and growth to test predictions

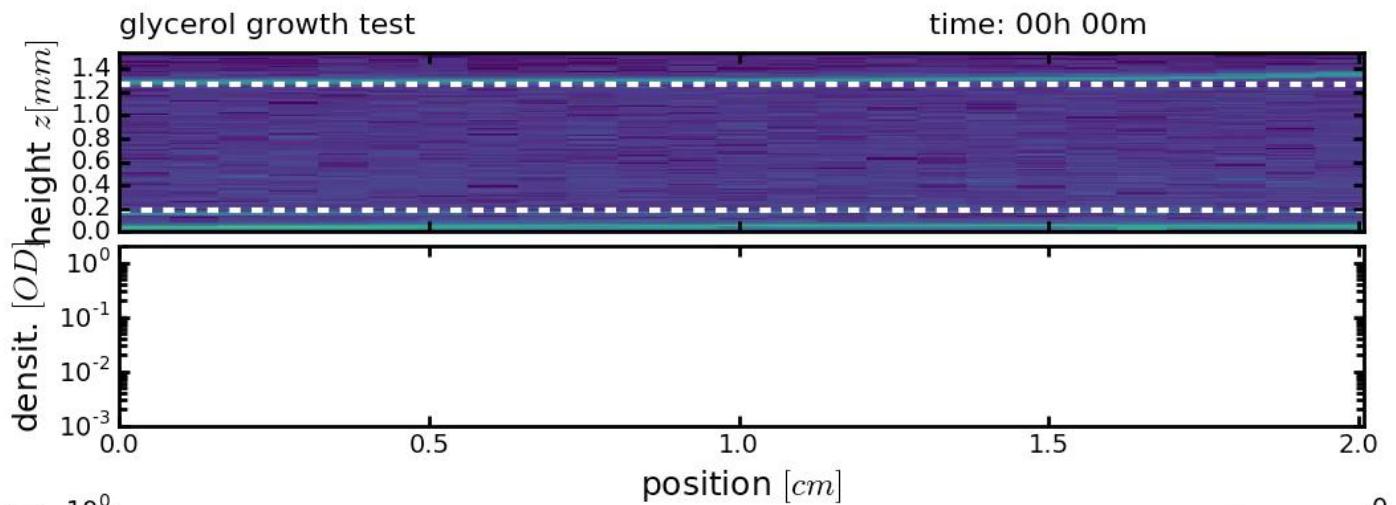
expansion speed:  $u_{FK} = 2\sqrt{D \cdot \lambda}$

slope expansion front:  $k = \sqrt{\frac{D}{\lambda}}$

# Determine growth rate



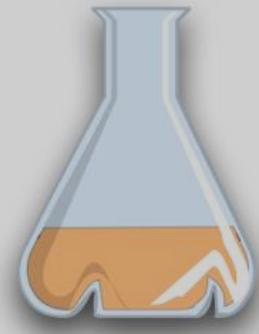
condition: glycerol, no attractant



→ Growth rate  $\lambda : 0.59 \text{ 1/h}$

# Side remark: Growing cells swim

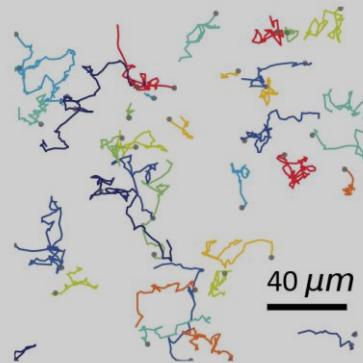
Measure swimming speeds for different conditions



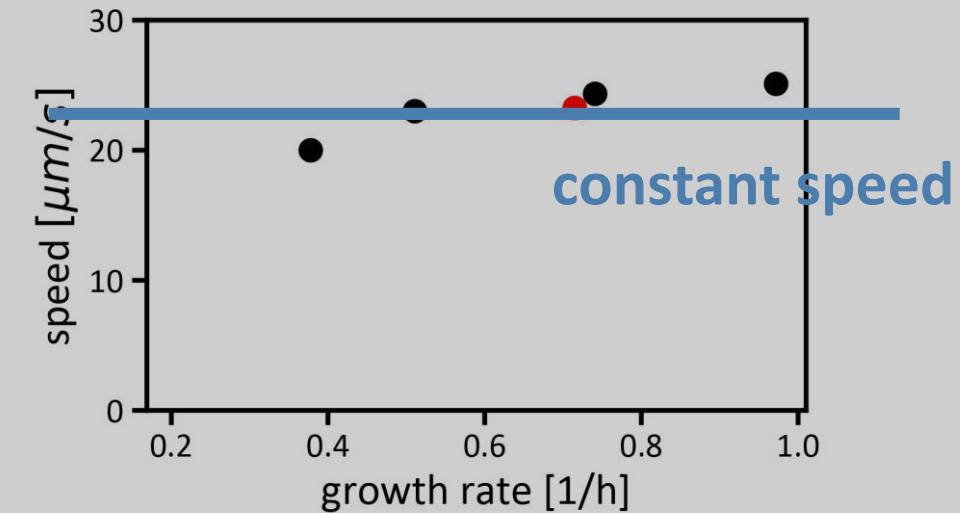
batch  
culture



microscopy



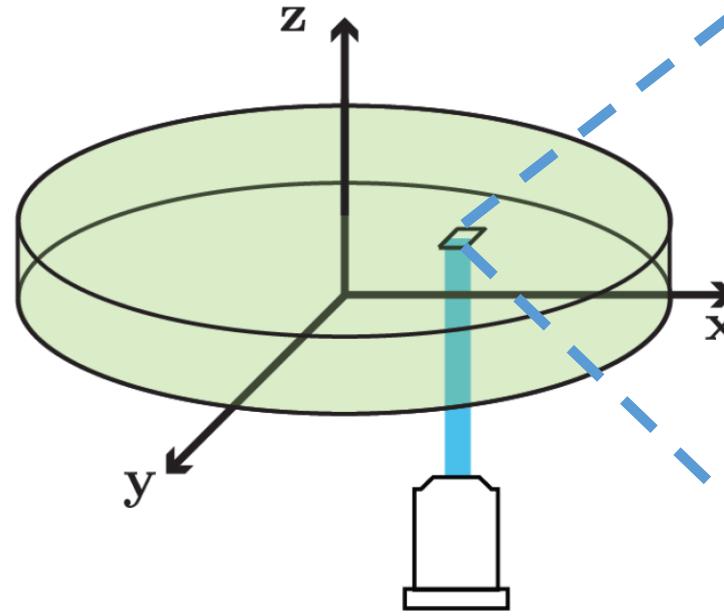
trajectory analysis



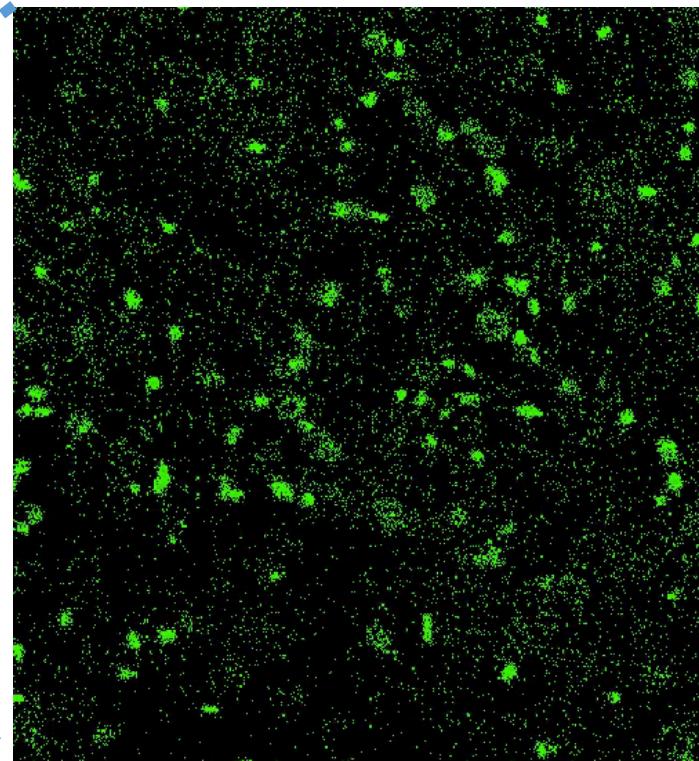
- Growing cells swim with constant speed, independent of exact growth condition
- Active regulation of swimming behavior

# Determine effective diffusion: direct measurement in soft-agar

cells in soft-agar

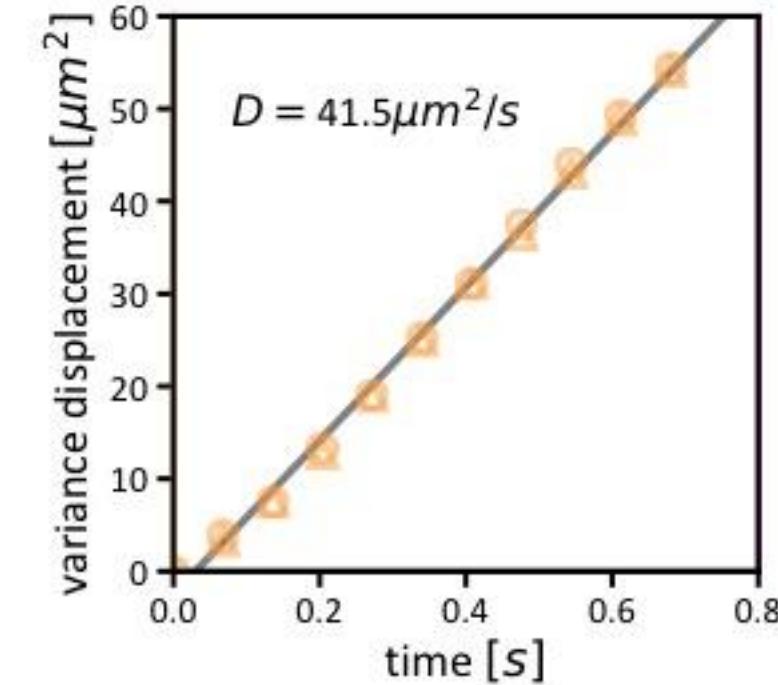


200 x 200  $\mu\text{m}$



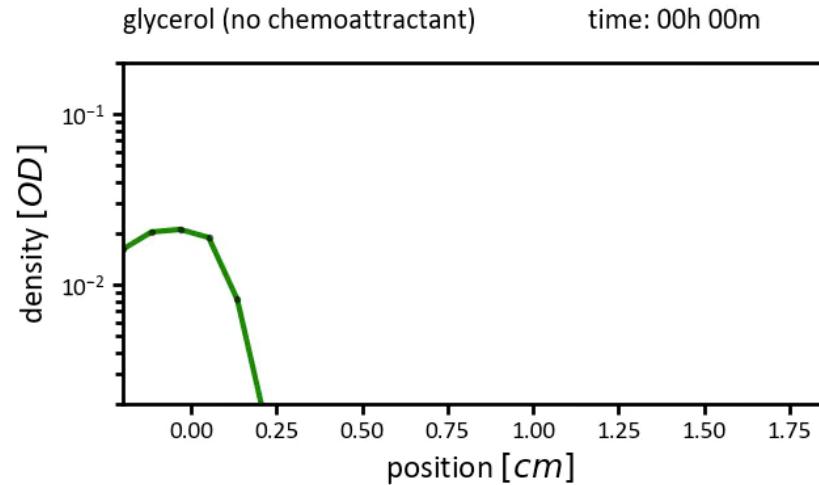
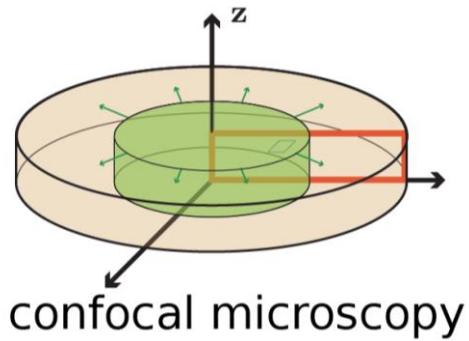
→ Diffusion  $D : 42 \mu\text{m}^2/\text{s}$

growth in glycerol

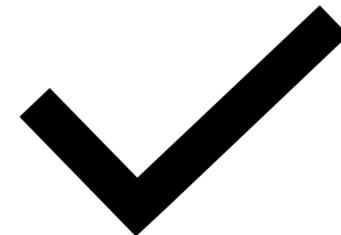
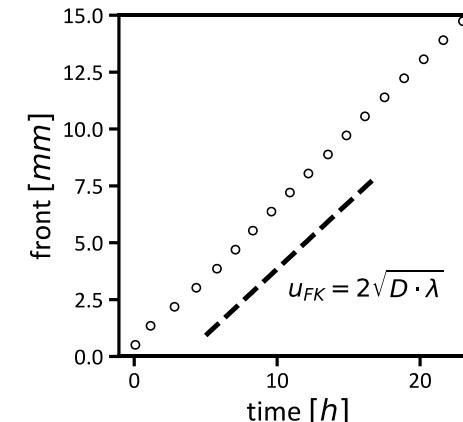
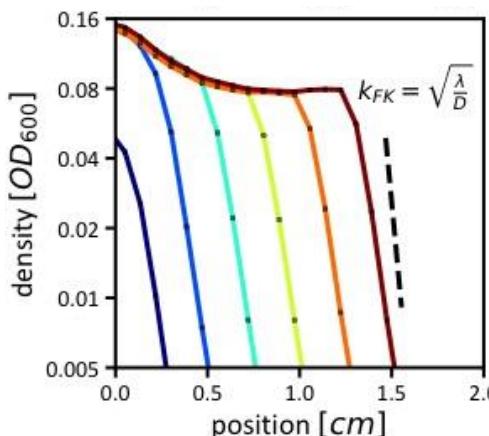


# Observed expansion without chemotaxis follows Fisher-Kolmogorov dynamics

## Observing expansion



## Comparison with theoretical prediction



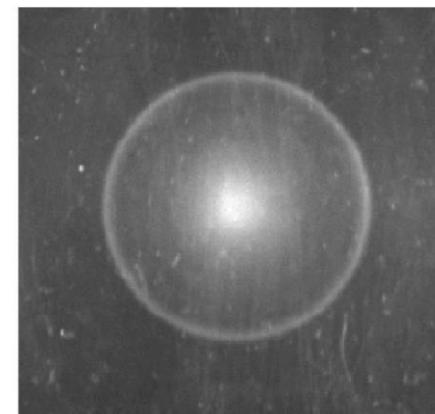
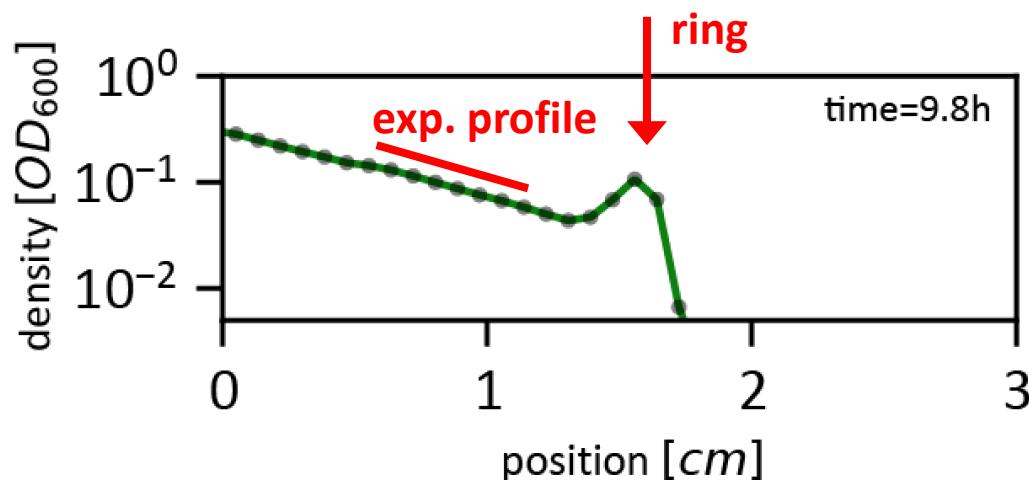
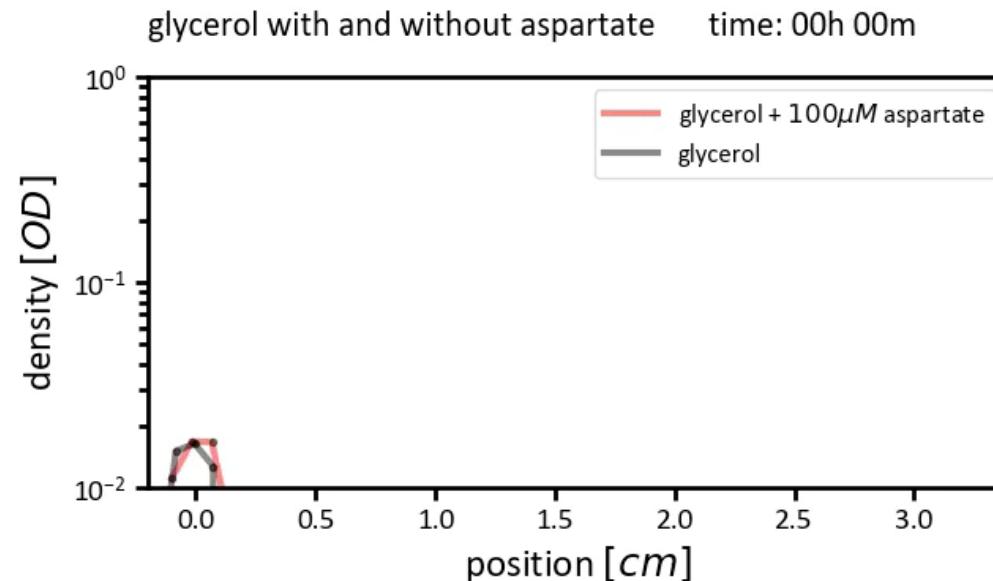
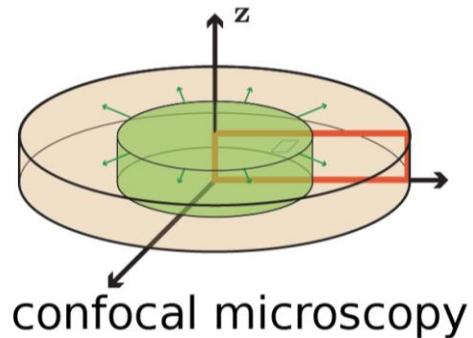
Fisher-Kolmogorov  
describes expansion

Back to chemotaxis

Experimentally: glycerol + aspartate

# Expansion with chemotaxis: ring and exponential trailing profile

## Observing expansion



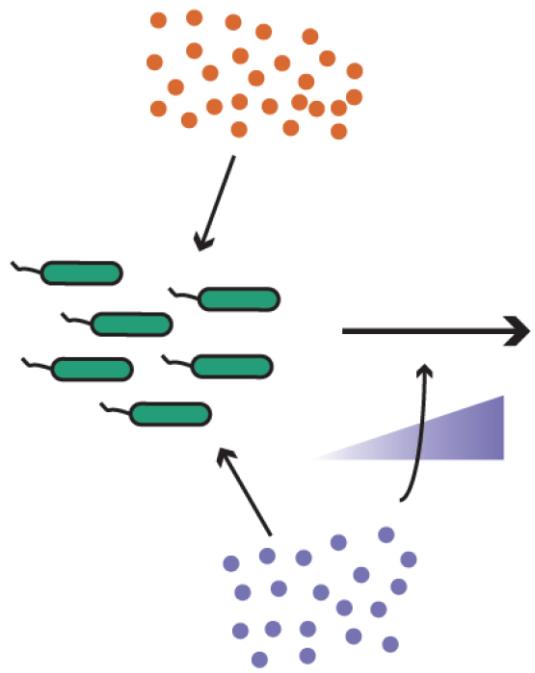
fast expansion:  
3.7 mm/h  
FK: 0.9 mm/h  
Colony: 0.1 mm/h

# A new model to describe chemotactic expansion

nutrients  
 $n(r, t)$

cells  
 $\rho(r, t)$

attractant  
 $a(r, t)$



$$\partial_t n = -\frac{\lambda(n, a)}{Y} \rho + D_n \Delta n$$

$$\partial_t \rho = -\nabla \cdot [v \rho] + D \Delta \rho + \lambda(n, a) \rho$$

$$v = \chi_0 \nabla \log \left[ \frac{1 + a/a_-}{1 + a/a_+} \right] \approx \chi_0 \frac{\nabla a}{a}$$

in sensible range

$$\partial_t a = -\mu \rho + D_a \Delta a$$

Crucial modifications of previous models:

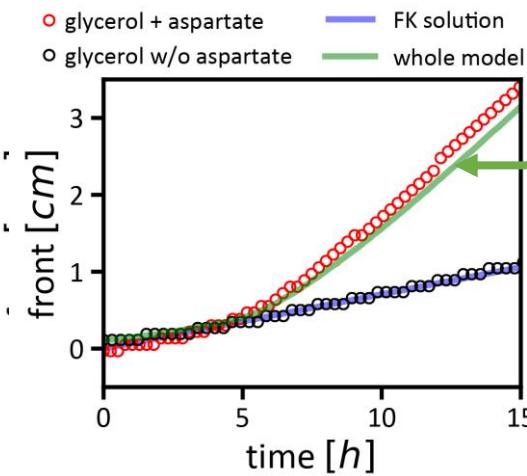
- Includes cell growth
- Separation between nutrient and attractant field

Only one fitting parameter:

$\chi_0$

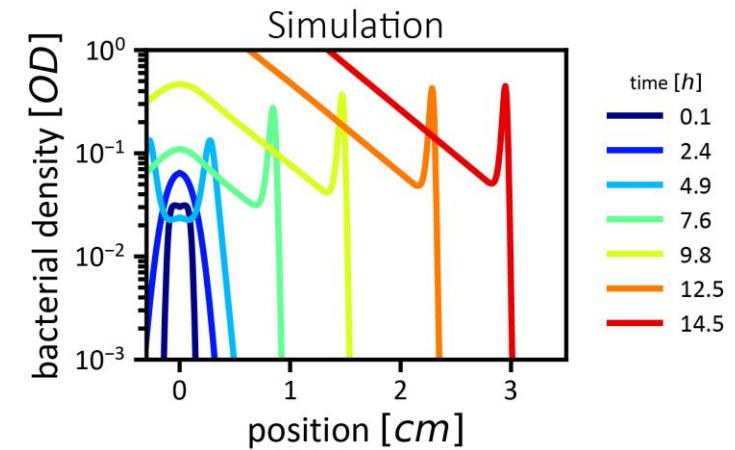
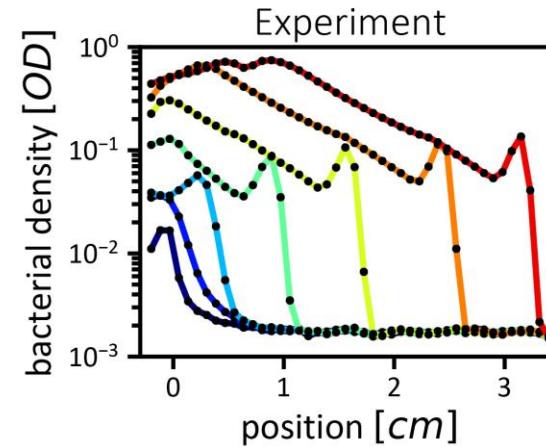
# Model predicts expansion dynamics

## Reference condition: glycerol + aspartate

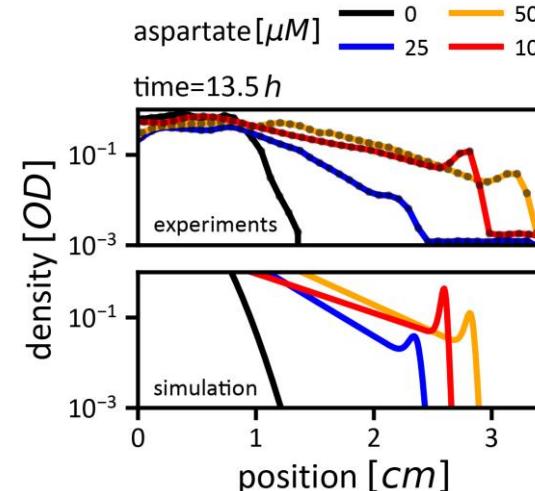
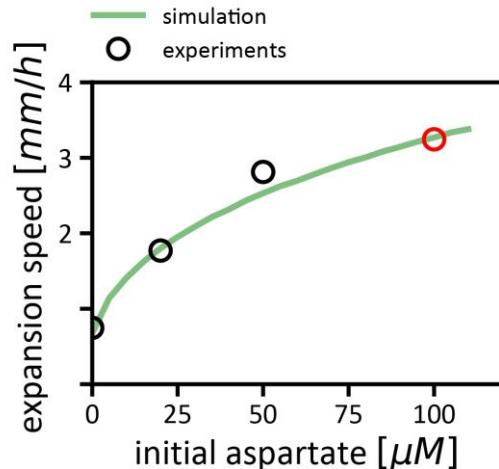


expansion speed  
matched by fitting

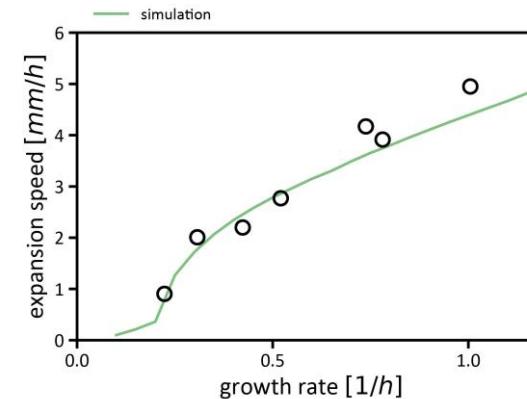
$$\chi_0$$



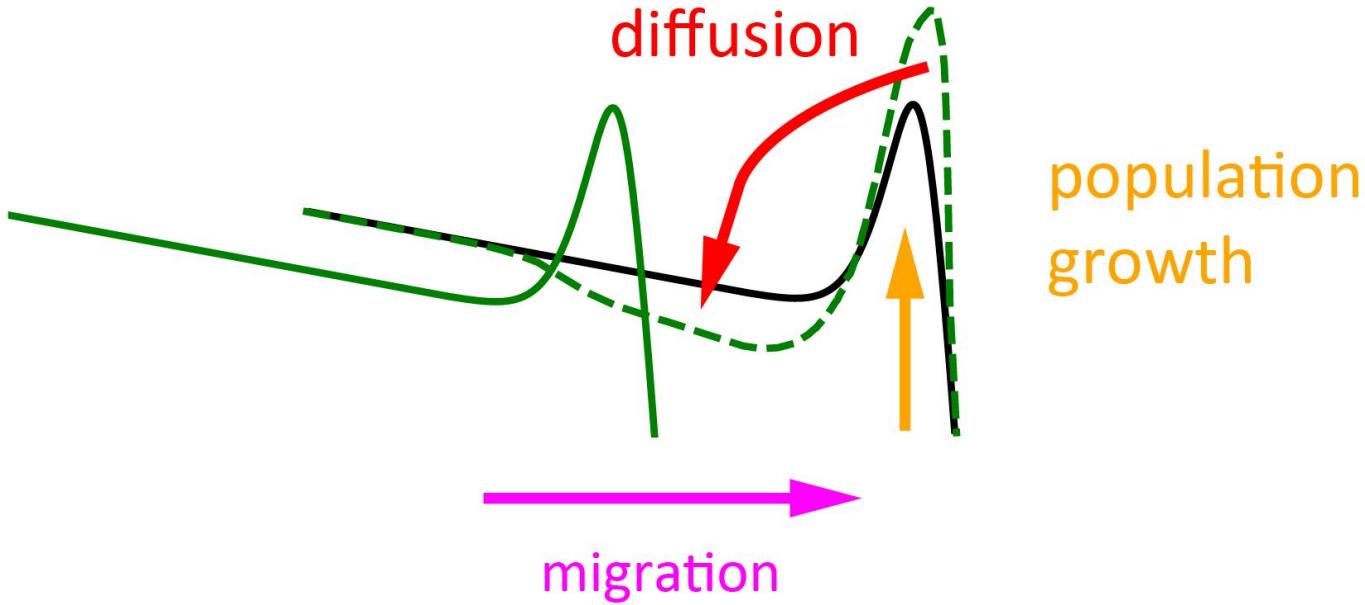
## Change in chemoattractant concentration



## Change in growth rate

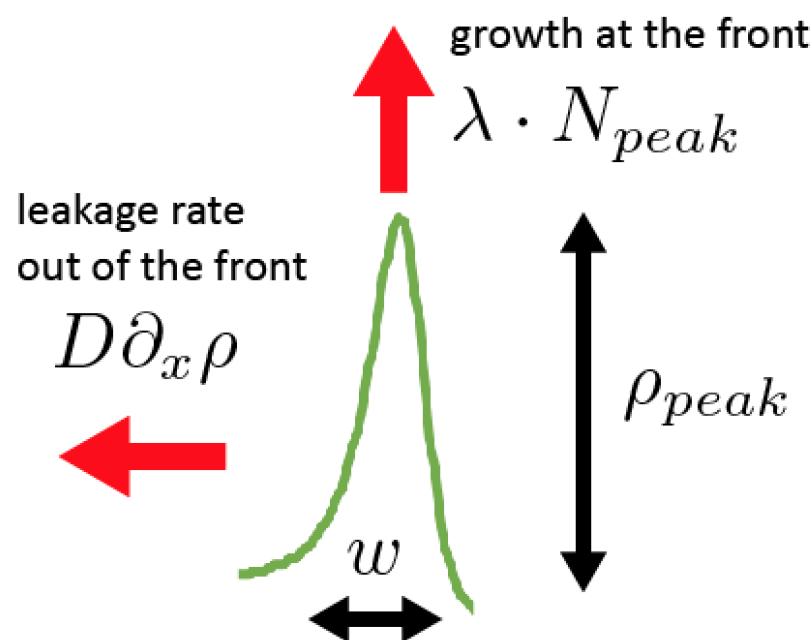


# Mode of expansion dynamics



- Growth at front is balanced by diffusion to the back.
- This leads to an efficient seeding of the trailing region
- Growth at the trailing region leads to an exponentially increasing profile

# A scaling theory of chemotactic expansion



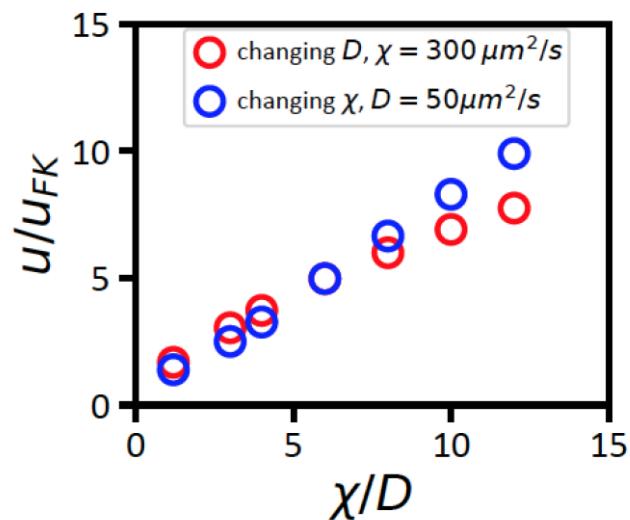
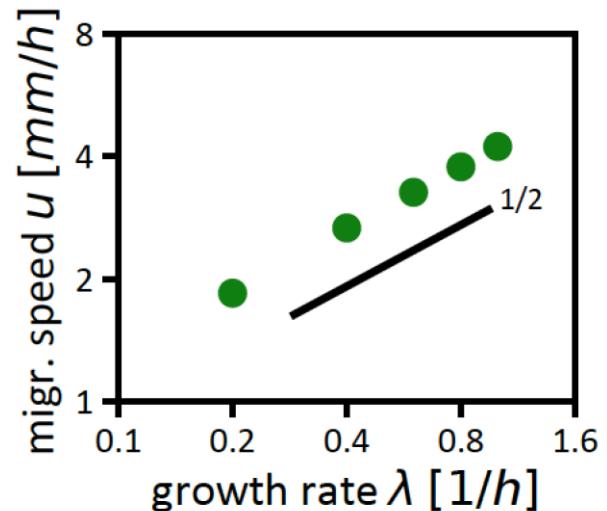
$$N_{peak} \sim \rho_{peak} \cdot w$$

$$\lambda \cdot N_{peak} \sim D \cdot \rho_{peak}/w$$

$$u \sim \chi/w$$

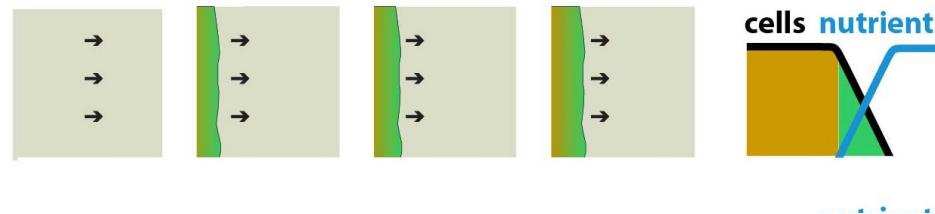
$$u \sim (\chi/D) \sqrt{D \cdot \lambda}$$

→ Chemotactic range expansion boost expansion speed

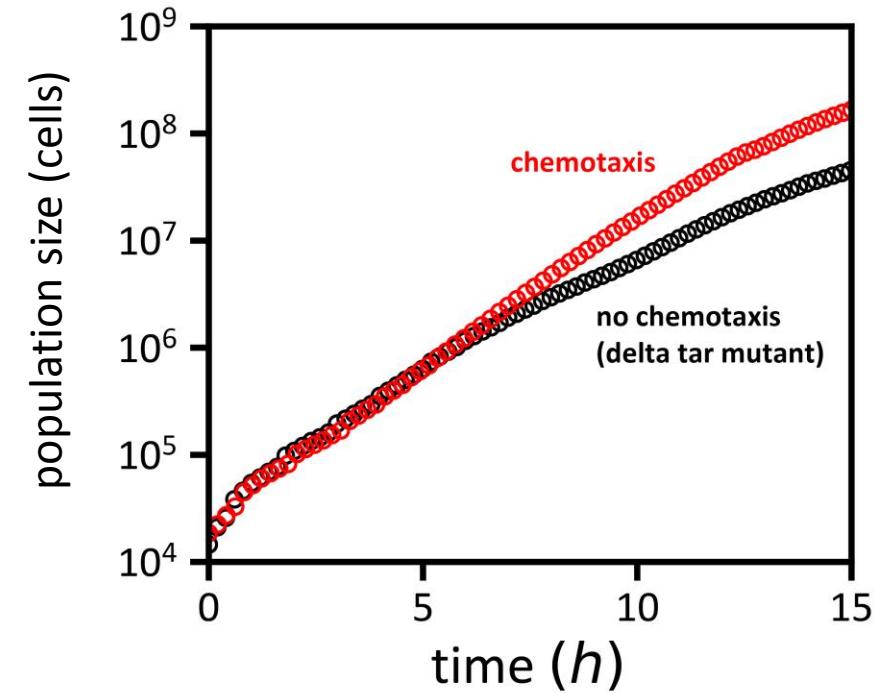
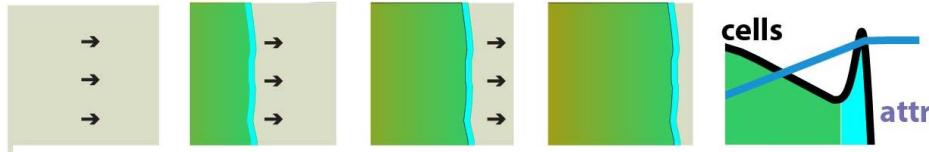


# Summary: Chemotaxis as growth strategy to thrive in nutrient-replete environments

unguided range expansion (FK)



navigated range expansion (chemotaxis)



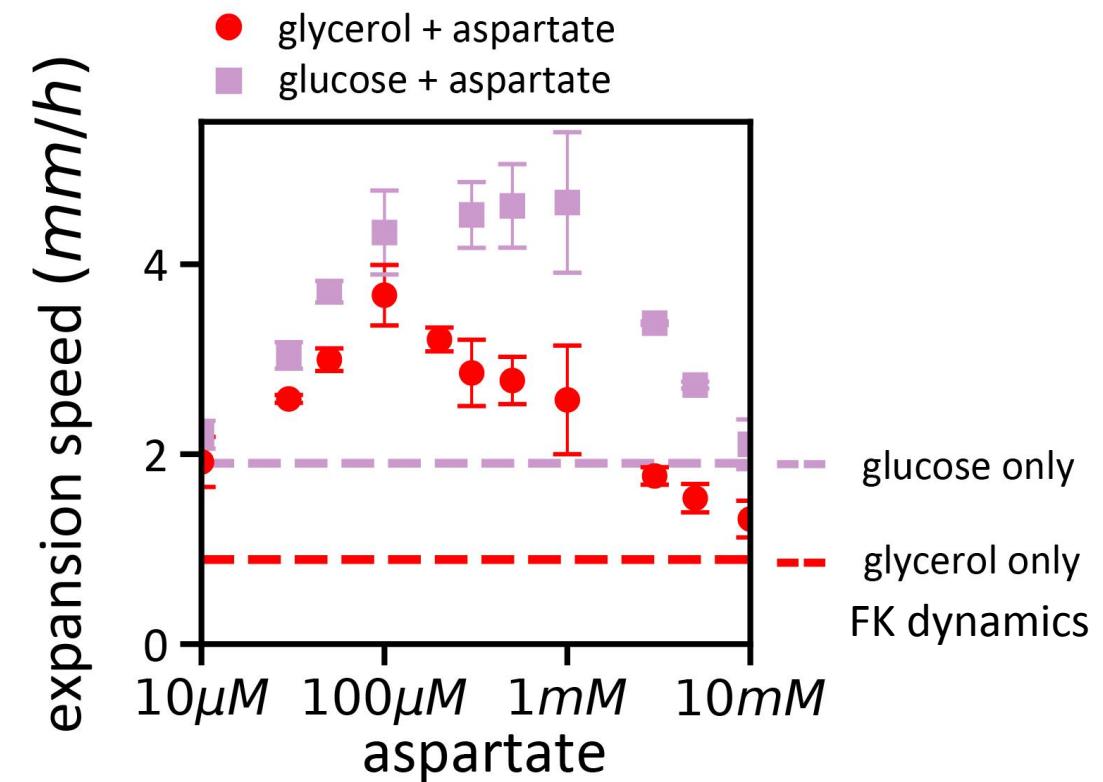
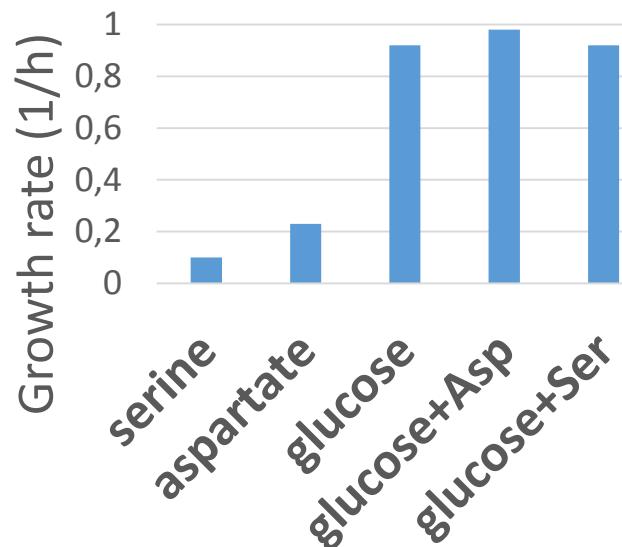
Chemotaxis leads to fast expansion via self-generated gradients and is an efficient strategy to grow in nutrient replete environments

# Non-nutritious attractants as cues for navigated range expansion

- A nutrient alone which can be sensed is only weakly increasing expansion speed:

$$u \sim \sqrt{\chi \cdot \lambda}$$

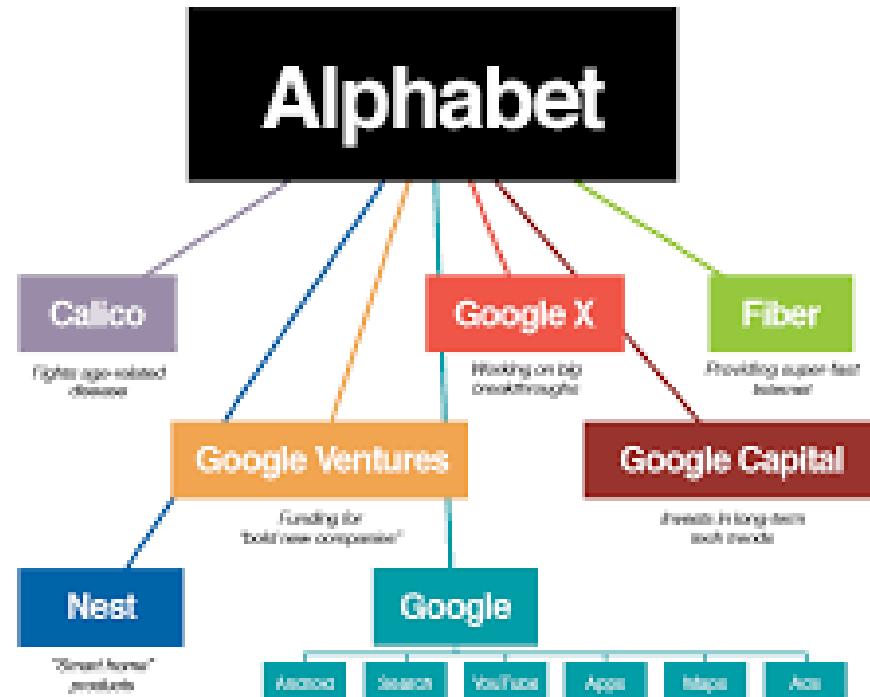
- Separation of nutrient and attractant speeds up migration:  $u \sim \chi \cdot \sqrt{\lambda}$
- Good attractants are not good nutrients but rather cues to boost range expansion.



# Oversimplified summary

Canonical hypothesis: nutrient foraging during starvation

Alternative (non-exclusive) hypothesis:  
range expansion during good growth conditions (diversification)



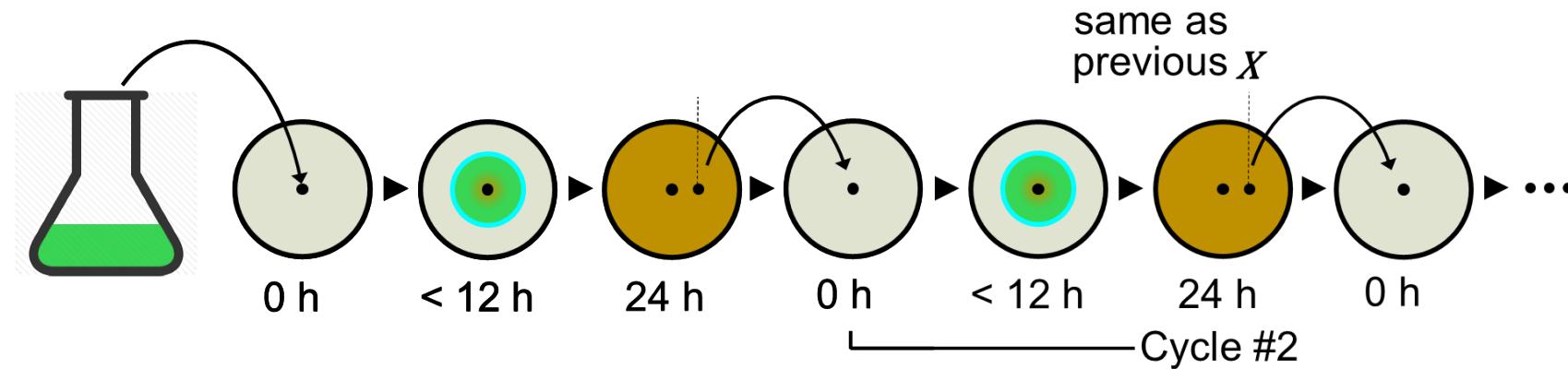
Is there an optimal swimming speed and expansion behavior?

If expansion via chemotaxis increases population growth:

Why are cells not expanding even faster?

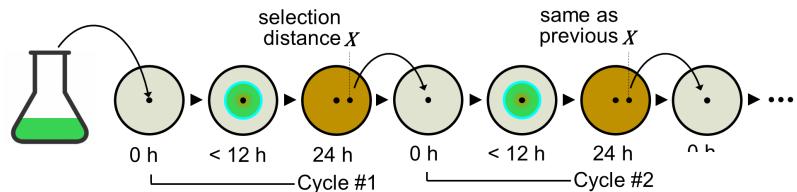
# Evolutionary study of swimming behavior

Introduce space dependent selection

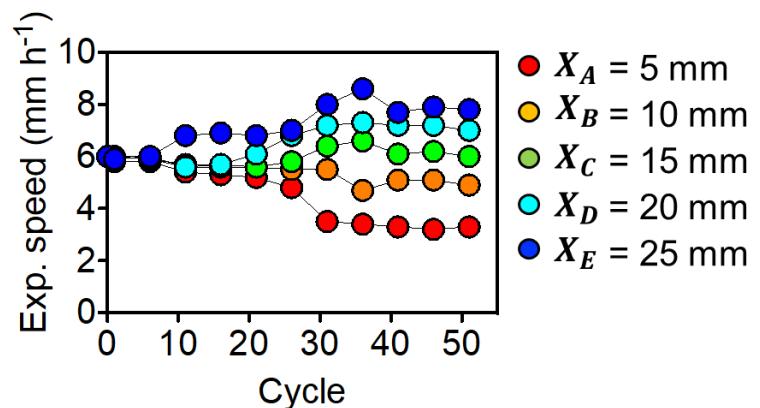


# Evolutionary study of swimming behavior

Introduce space dependent selection



Evolution depends on selection distance

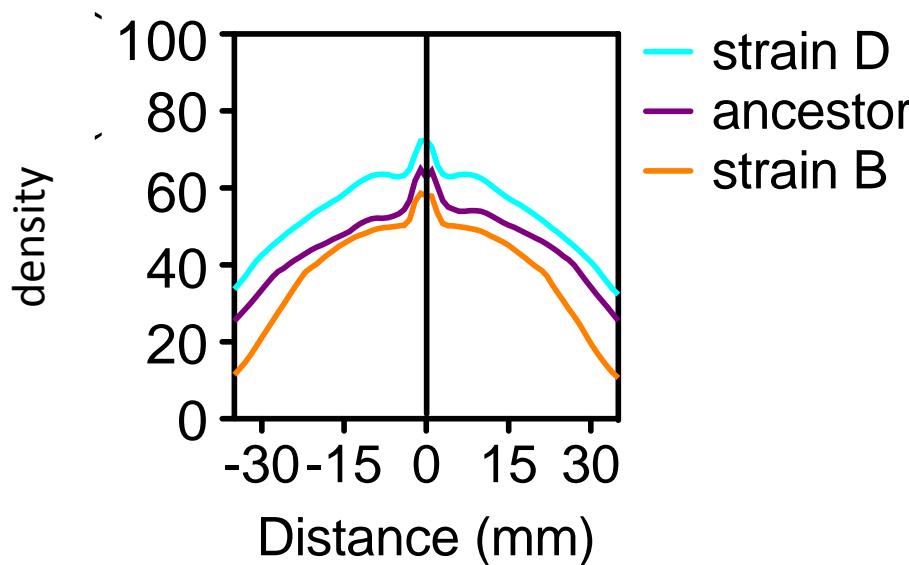


**Fast swimming is not always good: optimal swimming depends on typical habitat size cells encounter**

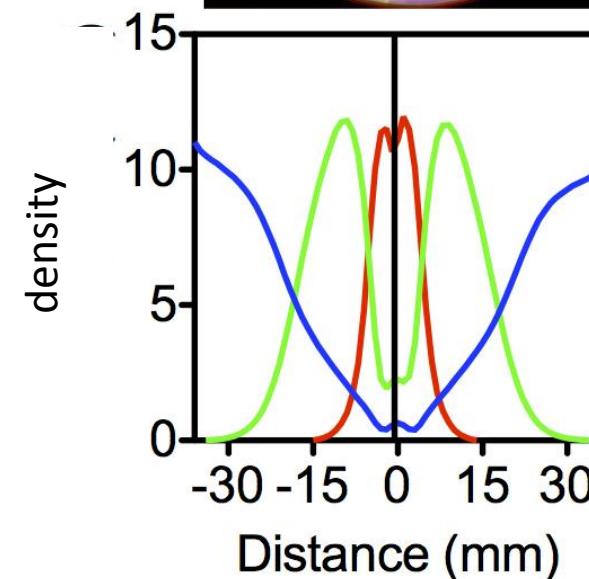
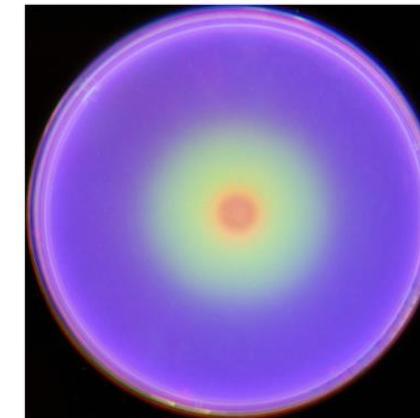
# Competition drives local abundance and selection dynamics

## Separate expansion

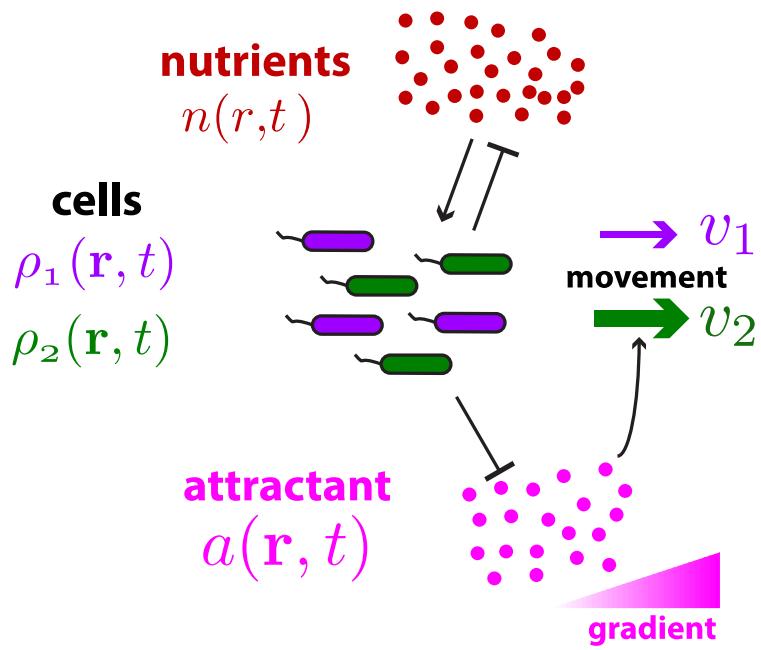
	strain	ES (mm/h)	GR (1/h)
fast	str. D	7.02	1.96
	anc.	5.92	1.98
slow	str. B	4.32	1.92



## Direct competition



# Modeling dynamics



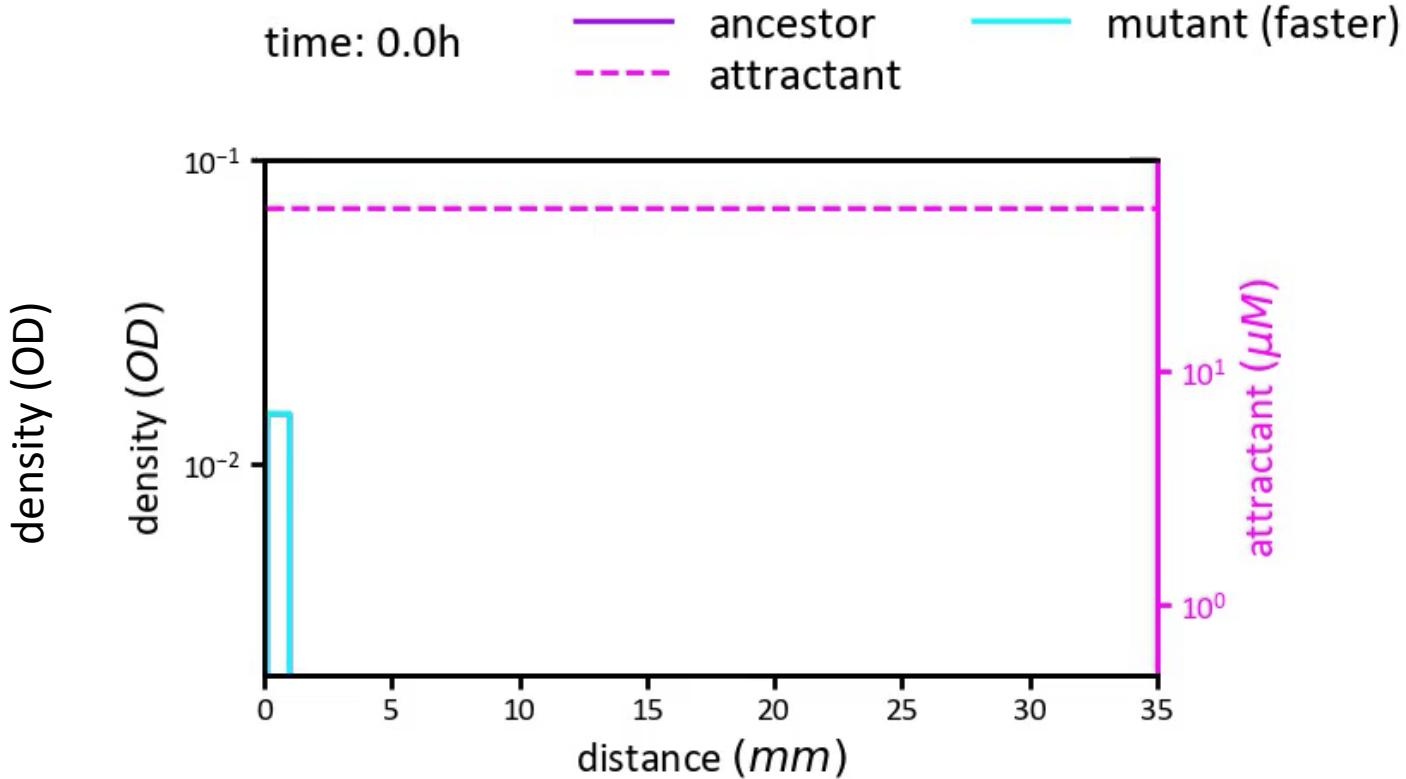
$$\partial_t \rho_1 = D_1 \Delta \rho_1 - \nabla \cdot (\mathbf{v}_1 \rho_1) + \lambda(n) \cdot \rho_1$$

$$\partial_t \rho_2 = D_2 \Delta \rho_2 - \nabla \cdot (\mathbf{v}_2 \rho_2) + \lambda(n) \cdot \rho_2$$

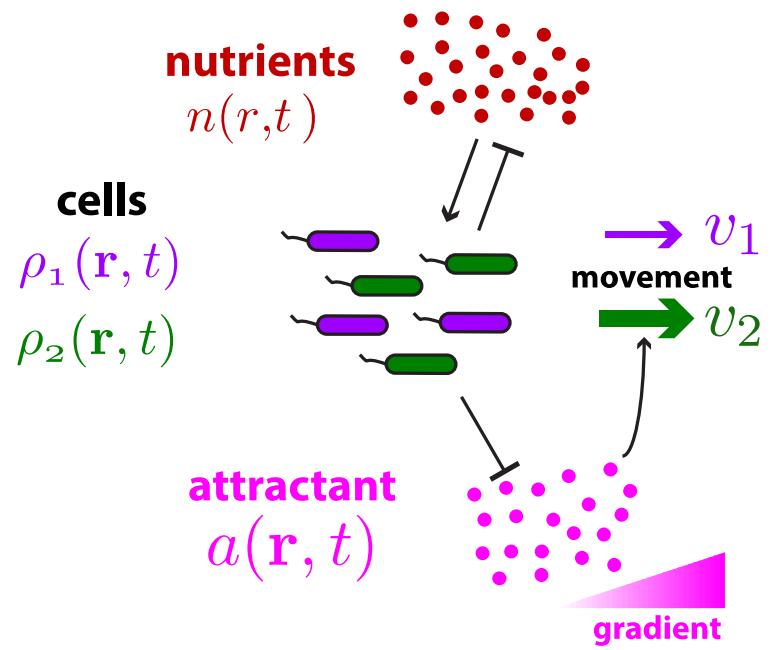
$$\mathbf{v}_{1,2} = c_{1,2} \nabla \log \left( \frac{1 + a/K_I}{1 + a/K_A} \right)$$

$$\partial_t a = D_0 \Delta a - \mu(a) \cdot (\rho_1 + \rho_2)$$

$$\partial_t n = D_0 \Delta n - \lambda(n) \cdot (\rho_1 + \rho_2)/Y_n$$



# Modeling dynamics



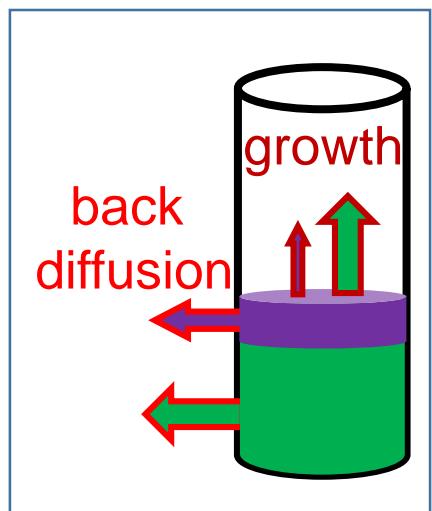
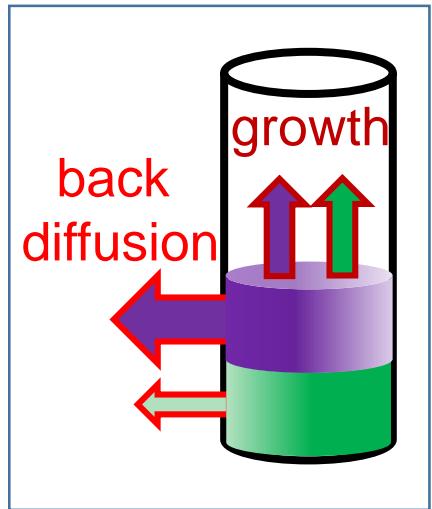
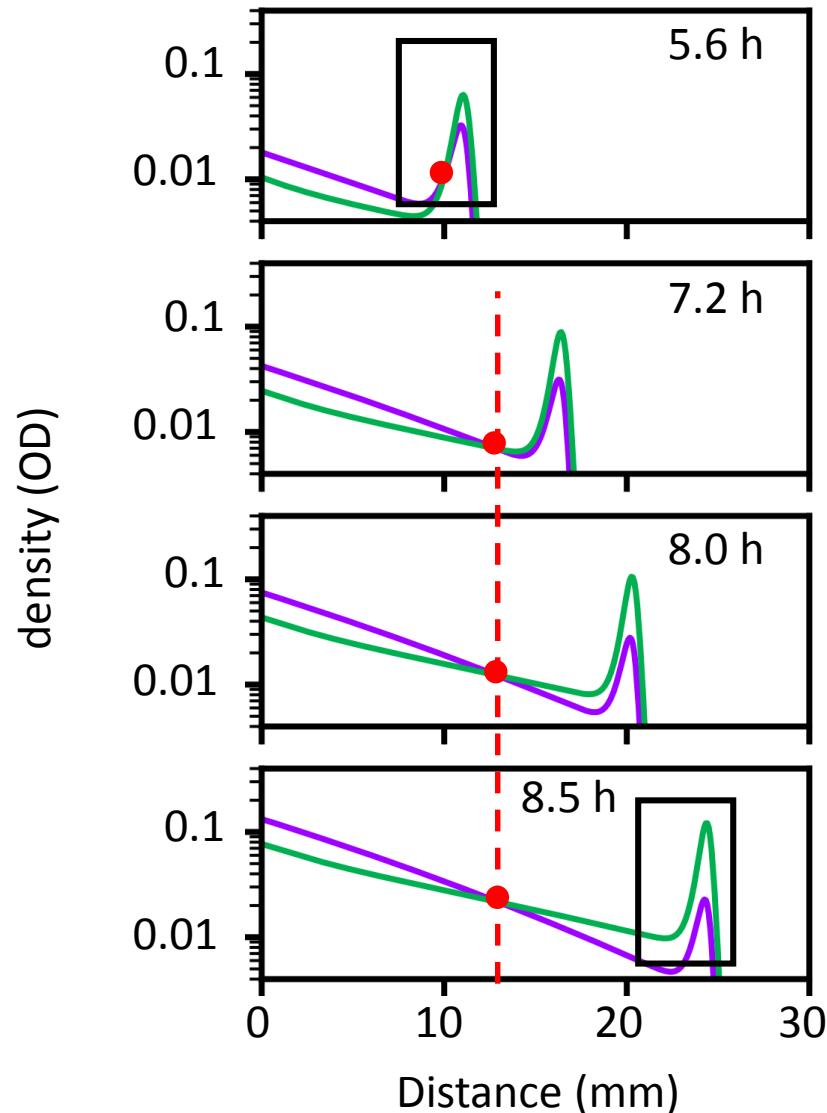
$$\partial_t \rho_1 = D_1 \Delta \rho_1 - \nabla \cdot (\mathbf{v}_1 \rho_1) + \lambda(n) \cdot \rho_1$$

$$\partial_t \rho_2 = D_2 \Delta \rho_2 - \nabla \cdot (\mathbf{v}_2 \rho_2) + \lambda(n) \cdot \rho_2$$

$$\mathbf{v}_{1,2} = c_{1,2} \nabla \log \left( \frac{1 + a/K_I}{1 + a/K_A} \right)$$

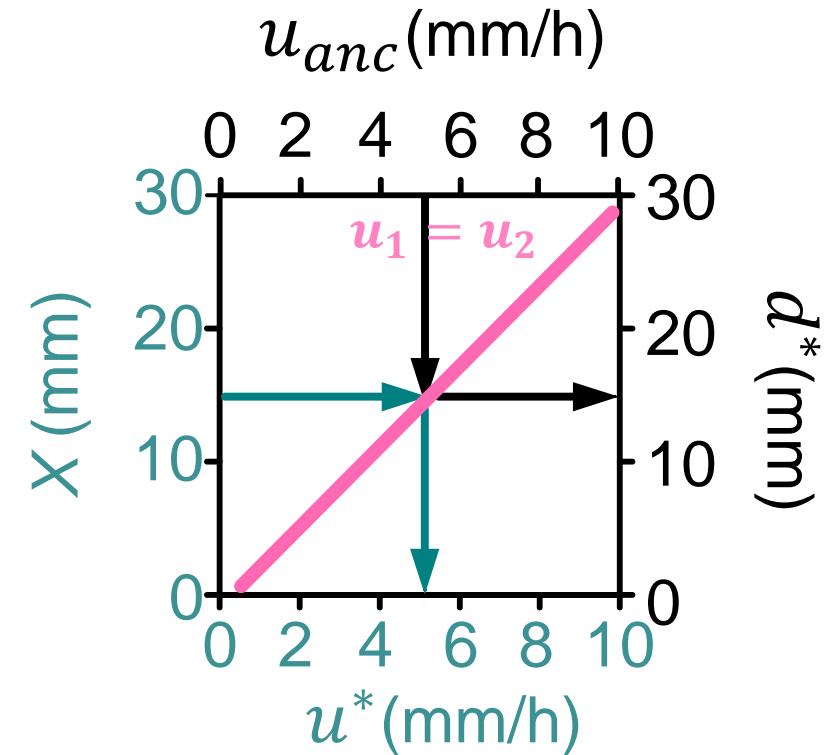
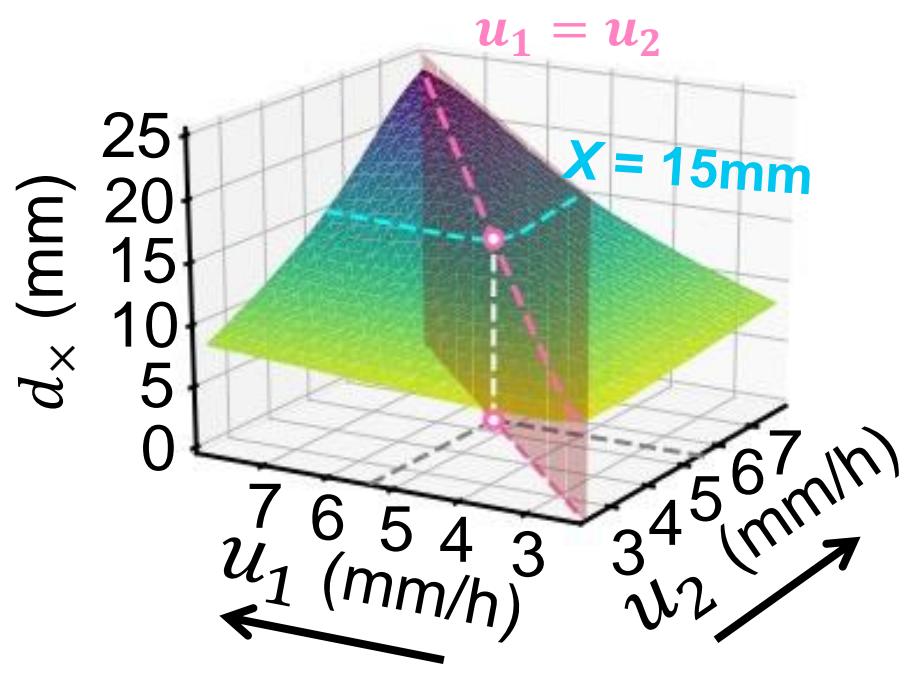
$$\partial_t a = D_0 \Delta a - \mu(a) \cdot (\rho_1 + \rho_2)$$

$$\partial_t n = D_0 \Delta n - \lambda(n) \cdot (\rho_1 + \rho_2) / Y_n$$



# Stable attractor of evolution

analyzing different expansion speeds



predicted stable attractor:

$$u^*(X) \propto X \cdot \lambda.$$

stable expansion speed

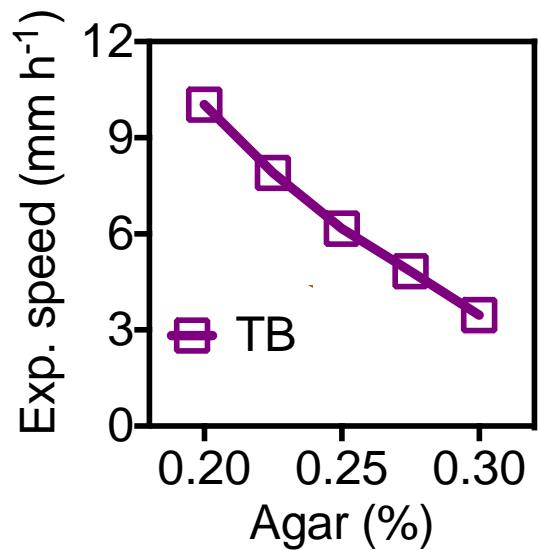
position growth-rate

# Test model prediction

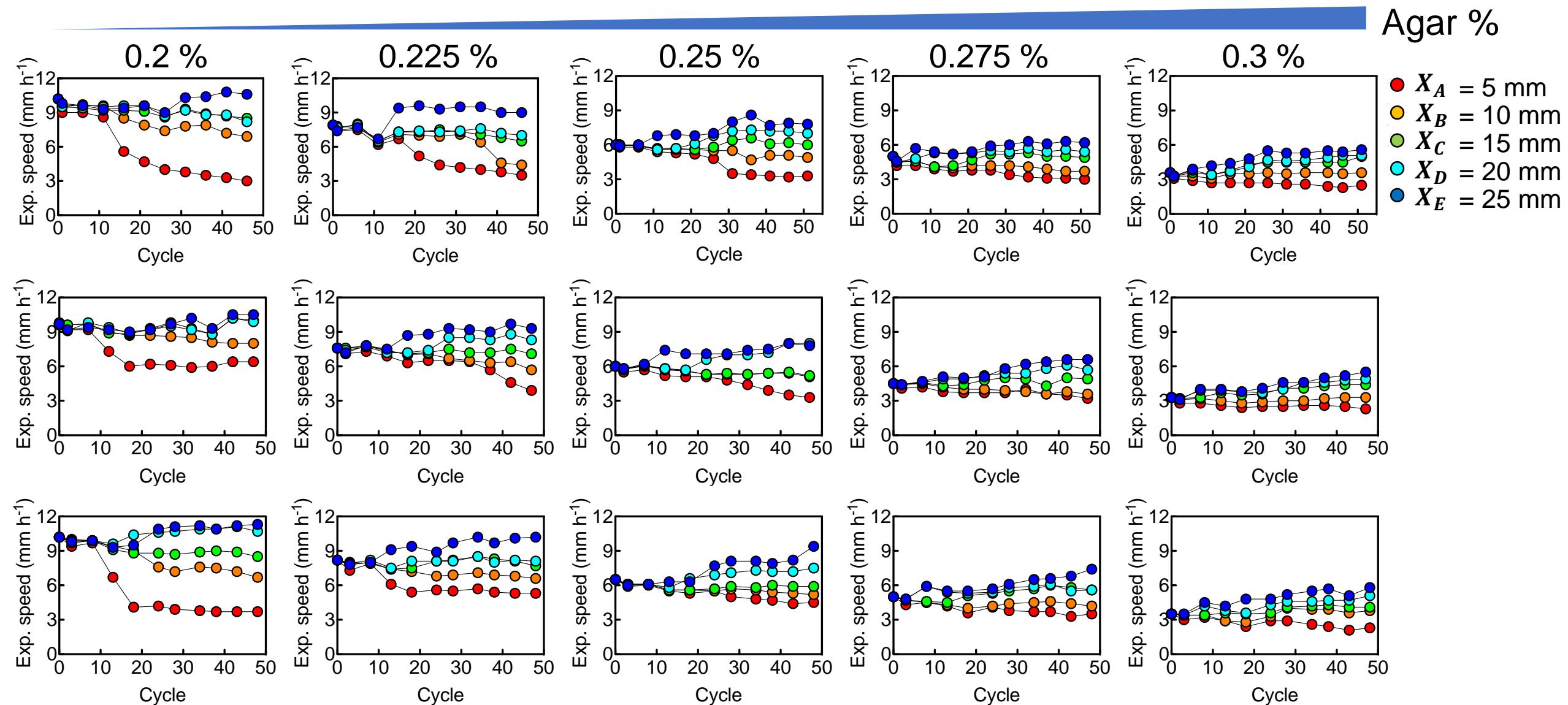
predicted stable attractor:

$$u^*(X) \propto X \cdot \lambda.$$

stable expansion speed      position    growth-rate



# Evolution in different agar concentrations

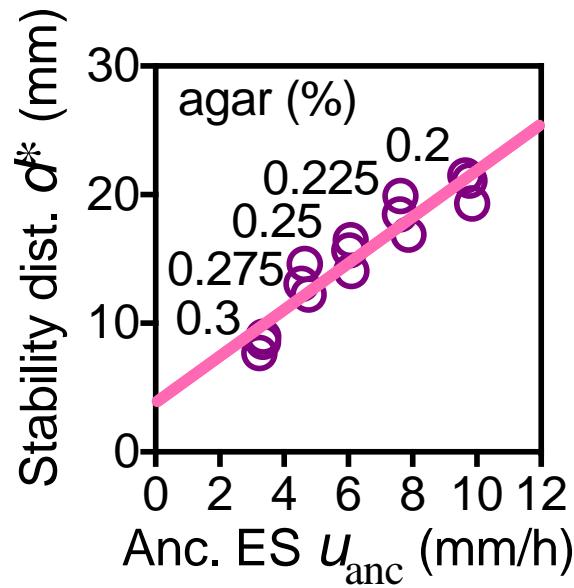
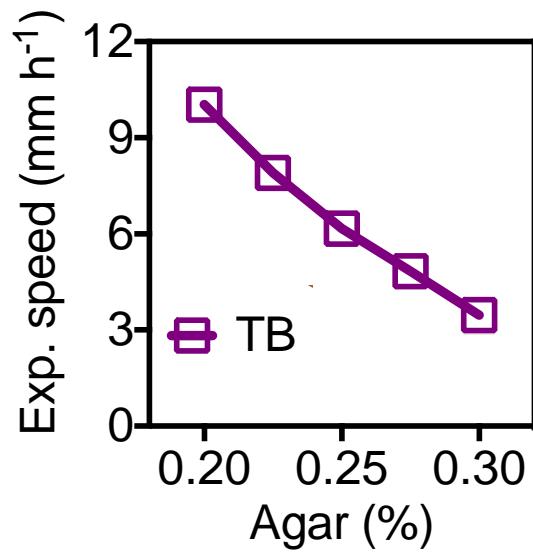


# Test model prediction

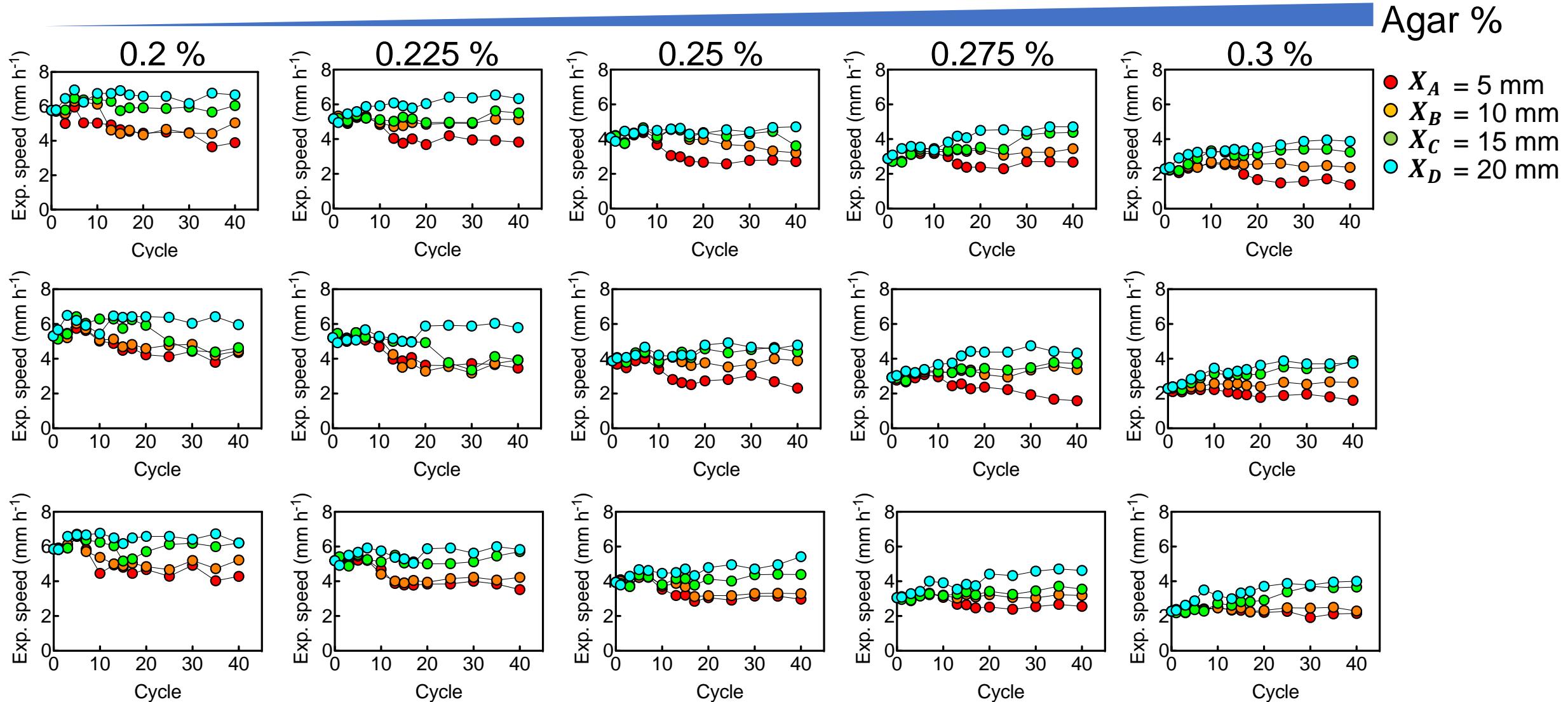
predicted stable attractor:

$$u^*(X) \propto X \cdot \lambda.$$

stable expansion speed      position      growth-rate



# Evolution in Casamino acids (slower growth)

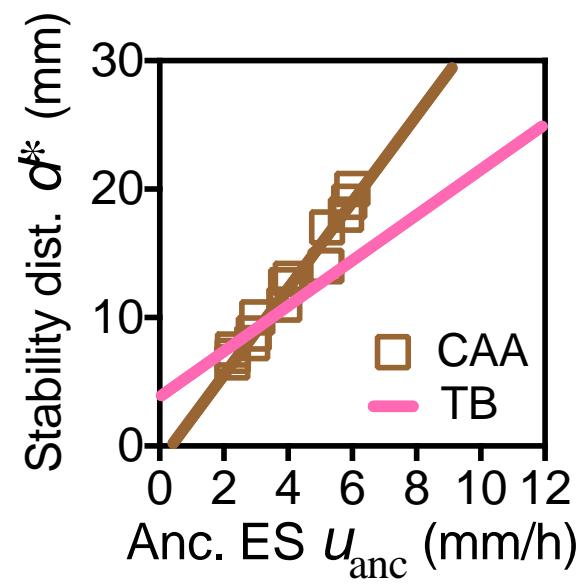
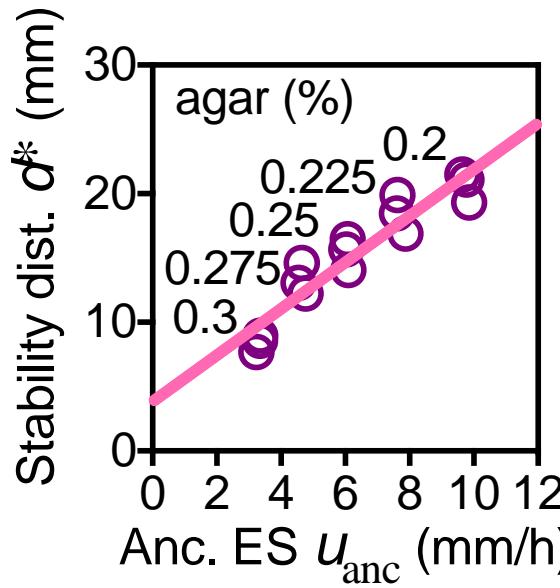
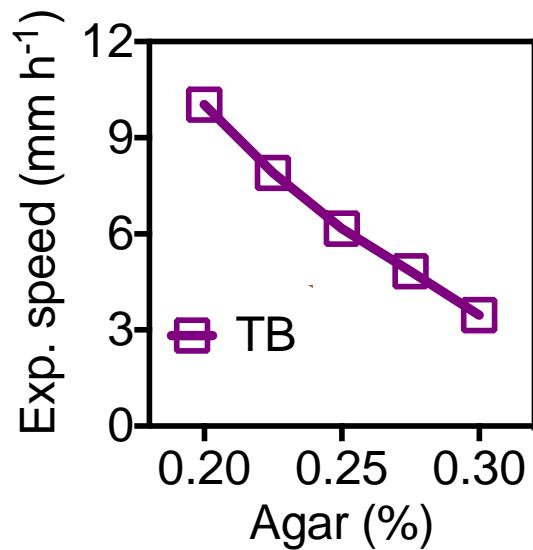


# Test model prediction

predicted stable attractor:

$$u^*(X) \propto X \cdot \lambda.$$

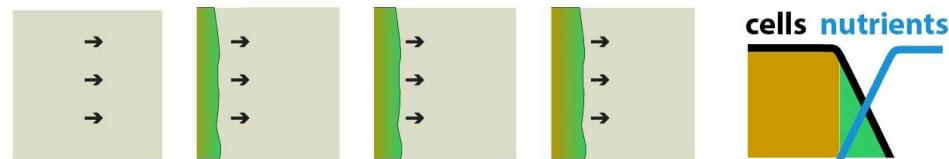
stable expansion speed      position      growth-rate



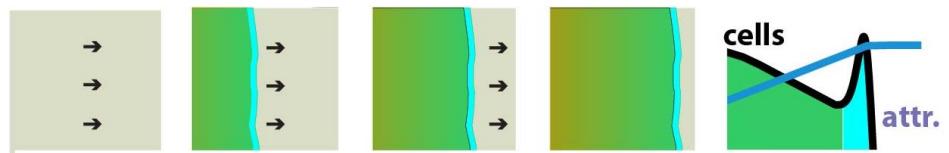
# Summary: Chemotaxis as growth strategy to thrive in nutrient-replete environments

Consumption of non-nutritious attractants leads to fast expansion and is an effective strategy to boost colonization into nutrient replete environments

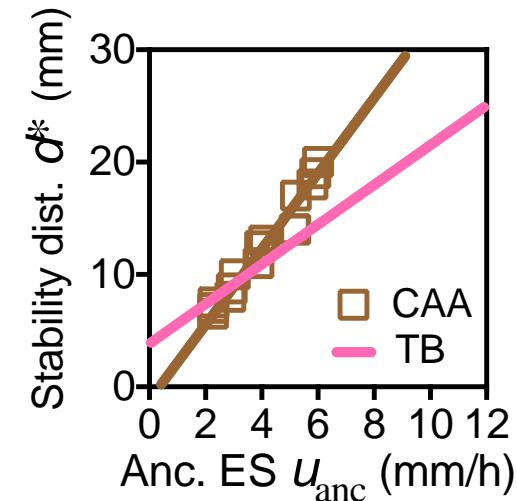
unguided range expansion (FK)



navigated range expansion (chemotaxis)



Competition leads to an optimal expansion speed which depends on habitat size



$$u^*(X) \propto X \cdot \lambda$$

stable expansion speed      size      growth-rate

Cremer, Honda, Tang, Wong-Ng, Vergassola, Hwa. Nature (2019)

Liu, Cremer, Li, Hwa, Liu. Nature (2019)

# Thank you for your attention!

Postdoc positions available. Contact me for further details.