W decay: W-> e_+ UR

$$\chi' = \begin{pmatrix} 0 & \sigma' \\ \sigma' & 0 \end{pmatrix}, \quad \chi'' = \begin{pmatrix} 0 \\ 10 \end{pmatrix}, \quad \chi_S = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$$

· helicity of massless left - handed state

$$\psi_{R} = \begin{pmatrix} 0 \\ u_{R} \end{pmatrix}, \quad \psi_{L} = \begin{pmatrix} u_{L} \\ 0 \end{pmatrix}, \quad \psi = \begin{pmatrix} u_{L} \\ u_{R} \end{pmatrix}$$
(2)

m=0 => 1/4=0

$$\Rightarrow \begin{pmatrix} 0 & / \circ - \overrightarrow{/} \cdot \overrightarrow{\sigma} \\ / \circ + \overrightarrow{/} \cdot \overrightarrow{\sigma} & 0 \end{pmatrix} \begin{pmatrix} u_L \\ u_R \end{pmatrix} = 0$$
(3)

$$\Rightarrow (p_0 - \overline{p} \cdot \overline{\sigma}) u_R = 0 ; (p_0 + \overline{p} \cdot \overline{\sigma}) u_L = 0$$

$$(4)$$

$$hu_{L} = -1/2 u_{L}$$
 $hu_{R} = 1/2 u_{R}$
 (5)

$$h \equiv \vec{s} \cdot \vec{p} = \vec{s} \cdot \vec{F} = \frac{\vec{\sigma}}{2} \cdot \vec{F} \qquad (p^{\circ} = |\vec{F}|)$$

left - handed fermions:
$$h = -1/2$$
 ($\vec{s} = 1/\vec{l}$)

with - -11 - ! $h = 1/2$ ($\vec{s} = 1/\vec{l}$)

· Polarization vectors of W-Loom:

$$\mathcal{E}_{pT}^{(1)} = \frac{1}{\sqrt{2}} \left(0; +1, +i, 0\right) / \sqrt{2}$$

$$\mathcal{E}_{pT}^{(2)} = \frac{1}{\sqrt{2}} \left(0; +1, -i, 0\right) / \sqrt{2}$$
vert-frame
$$\mathcal{E}_{pL}^{(3)} = \left(0; 0, 0, 1\right)$$
(6)

Notice:
$$\sum_{i} \epsilon_{n}^{(i)} \epsilon_{v}^{(i)*} = -g_{nv} + \frac{k_{r}k_{v}}{m^{v}} (7)$$

$$\left(\begin{array}{c} h^{o} = m, & h^{i} = 0 \end{array} \right)$$

•
$$(T_i)_{jk} = -i \, \Sigma_{ijk} \quad \text{give} : \quad [T_i, T_j] = i \, \Sigma_{ijk} \, T_k$$

generators of $SU(2)$
 $\text{fw the triplet (vector)}$
 $SO(3) = SU(2)$

(8)

$$\Rightarrow T_3 = \begin{pmatrix} 0 & -i & 0 \\ i & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

$$\Rightarrow T_3 \vec{\epsilon}_{\tau} = + \vec{\epsilon}_{\tau}^{(i)}$$

$$T_3 \vec{\varepsilon}_T^{(2)} = -\vec{\varepsilon}_T^{(2)}$$

$$T_3 \vec{\epsilon}_L^{(s)} = 8 0$$

$$= \sum_{\mu} \frac{(1)}{T} : corresponds to 4pin + 1 along the 7-exis (Sz=1)$$

$$\sum_{j=1}^{(2)} f_{j} = -1$$

$$\mathcal{E}_{LL}^{(3)}$$
: $\mathcal{L}_{+}=0$

· Boosty in Z-obvection:
$$E_z' = \frac{\varepsilon_z + v \varepsilon_0}{V_{1-v}}$$

$$\mathcal{E}_{t}' = \frac{\mathcal{E}_{t} + \sqrt{20}}{\sqrt{1-v^{2}}}$$

$$\mathcal{E}_{0}' = \frac{\mathcal{E}_{0} + \sqrt{27}}{\sqrt{1-v^{2}}} \qquad (11)$$

$$p = \frac{mv}{\sqrt{1-v^2}}; \quad E = \frac{m}{\sqrt{1-v^2}}$$

$$= V = 1/E ; \frac{1}{\sqrt{1-v^2}} = E/m (12)$$

$$= \frac{\xi_{\mu T}^{(1)}}{\xi_{\mu T}} = \frac{\xi_{\mu T}^{(2)}}{\xi_{\mu T}}; \quad \xi_{\mu T}^{(2)} = \xi_{\mu T}^{(2)}$$

$$- \text{ trewsume planization } \left(\perp \overline{\mu} \right)$$

$$\mathcal{E}_{\mu}^{(3)} = \left(\frac{1\overline{\mu}1}{m}, 0, 0, \overline{\mu}\right) - l_{mpi} d_{mpi} d_{m$$

normalization:
$$\xi_{\mu}^{(i)} \xi_{\mu}^{(i)} = -1$$

Important comment

I tale
$$CT = (0, 1, \pm 1, 0)/\sqrt{2}$$

$$S_3 = \begin{pmatrix} 0 & -1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

Q. what dictates the form of S? why is $T_3 = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$ not good?

A. The cloice of Pauli motios.

$$Ai' = Ai' \neq Ae'j'u \Theta j Hu = Ai' + i \Theta j'T_j)iu Au$$

$$\Rightarrow \emptyset (T_i)ju = -1' \in j'u$$

Trace formulas

use:

Ched:

$$\gamma_{0} \gamma_{1} \gamma_{2} \gamma_{3} = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} \begin{pmatrix} \sigma_{1} & 0 \\ -\sigma_{1} & 0 \end{pmatrix} \begin{pmatrix} \sigma_{2} & 0 \\ -\sigma_{2} & 0 \end{pmatrix} \begin{pmatrix} \sigma_{3} & 0 \\ -\sigma_{3} & 0 \end{pmatrix} = \begin{pmatrix} \sigma_{1} \sigma_{2} \sigma_{3} & 0 \\ 0 & -\sigma_{1} \sigma_{2} \sigma_{3} \end{pmatrix}$$

$$\Rightarrow \gamma_{5} = \begin{pmatrix} 1 & 0 \\ 0 & -I \end{pmatrix} \begin{pmatrix} \sigma_{5} & \sigma_{5} & \sigma_{5} \\ 0 & -I \end{pmatrix} \begin{pmatrix} \sigma_{5} & \sigma_{5} \\ \sigma_{5} & \sigma_{5} \end{pmatrix} = \begin{pmatrix} \sigma_{5} \sigma_{5} & \sigma_{5} \\ \sigma_{5} & \sigma_{5} & \sigma_{5} \end{pmatrix}$$

$$\Rightarrow \gamma_{5} = \begin{pmatrix} 1 & 0 \\ 0 & -I \end{pmatrix} \begin{pmatrix} \sigma_{5} & \sigma_{5} \\ \sigma_{5} & \sigma_{5} \end{pmatrix} \begin{pmatrix} \sigma_{5} & \sigma_{5} \\ \sigma_{5} & \sigma_{5} \end{pmatrix}$$

$$|m|^2 = \frac{g^2}{2} \in_{\mu} \bar{n}(p) g^{\mu} L u(g) \bar{u}(g) g^{\nu} L u \in_{\nu}^{\dagger}$$
 $ent:-newtine$
 $electron of momentum p$ (momentum e)

next:
$$\sum_{q_i \mid m} |m|^2 = ?$$

$$4ne: \sum_{s} u \overline{u} = k$$

$$\sum_{s} v \overline{v} = k$$

$$\Rightarrow \sum_{s} |m|^{2} = 8\frac{1}{2} T_{v} \left[2 2 2 2 2 1 \right] = \frac{9}{2} T_{v} \left[2 2 2 2 2 \right]$$

$$(16)$$

$$\mathcal{E} = (0; +1, +i, 0) / \sqrt{2} \qquad (\int_{\frac{1}{2}}^{w} = +1)$$

$$\mathcal{E}^{*} = (0; +1, -1, 0) / \sqrt{2}$$

$$p_r = (1; \sin\theta, 0, \cos\theta) \frac{Hw}{2}$$

$$g = (1; -kn\sigma, 0, -cn\theta) \frac{Mw}{2}$$

$$T_{\nu} \notin \mathcal{X} = 4\left(\frac{M_{W}}{2}\right)^{2} \left[\frac{1}{2} \cdot 2\left(-s_{W}^{2} + 2\right) + 2\right]$$

(use:
$$\xi \cdot \ell = \frac{H_W}{2V_Z} + h_M \theta$$

 $\xi \cdot \gamma = \xi' \cdot \gamma = \frac{H_W}{2V_Z} + h_M \theta$
 $\gamma \cdot \ell = \frac{H_W}{4} \cdot 2$

(11/

limit:
(we = w, =0)

• To
$$\left[\cancel{\xi} \cancel{\xi} \cancel{\xi} \cancel{\xi} \right] = -4i \quad \xi_{\mu\nu\alpha\beta} \quad \xi^{\mu} 2^{3} \xi^{*} \cancel{\xi}^{\beta}$$

$$= + 2 H_{W}^{2} c_{0} 0 \qquad (19)$$

$$\frac{1}{2} \left[m \right]^{2} = \frac{g^{2}}{4} H_{W}^{2} \left[1 + c_{0}^{2} 0 - 2c_{0} 0 \right]$$

parity conserving

penty violation (85)

小

$$\frac{\sum |m|^2 = \frac{g^2 2}{4} M_W (1 - G_0 e)^2}{(20)}$$

Differential cross section

$$\frac{d\Gamma}{d\Omega} = \frac{1}{(2\pi)^2} \int \frac{1^2 dp}{2p_0} \int \frac{d^3 \ell}{2q_0} \frac{1}{24_0} \sum_{s} |m|^2 \delta^{(s)} (4-p-\ell)$$

$$k_0 = H_W, \quad \vec{h} = 0 \qquad (p = |\vec{p}|);$$

$$\ell = (\vec{\ell}|)$$

$$\frac{d\Gamma}{d\Omega} = \frac{1}{4\pi^2} \frac{g^2 H_W^2 (1-c_0 o)^2 \frac{1}{2H_W} \int \frac{1}{2H_W} \frac{\delta (H_W - 2p)}{2H_W}$$

Since:
$$\int \frac{d^3\ell}{270} \delta^{(3)}(\vec{p}+\vec{\ell}') = \frac{1}{2|\vec{p}|} = \frac{1}{2|p|}$$

Y,

$$\frac{d\Gamma}{d\Omega} = \frac{g + M_{W}}{4\pi^{2} \cdot 4 \cdot 2 \cdot 4} \frac{1}{2} \left(1 - G_{00}\right)^{2}$$

$$\frac{d\Gamma}{d\Omega}(\phi) = \frac{\int_{0}^{\infty} H_{W}}{256 \, \pi^{2}} \left(1 - G_{0}\phi\right)^{2} \tag{22}$$

Total decay rote

$$\Gamma = \int \frac{d\Gamma}{dx} dx = 2\pi \int \frac{d\Gamma}{dx} \sin x dx$$

$$\int_{W} = \frac{g^{2} M_{W}}{256 \pi^{2}} \cdot 2\pi \int_{0}^{\infty} 6 \pi o \, do \, (1 - 4 \pi o)^{2}$$

$$\Rightarrow \boxed{\Gamma_W(+1) = \frac{g^* M_W}{48\pi}} \qquad \qquad f_W S_z^W = +1$$

Must be equal = question of convention what is up and what is down

• Exercise:
$$\Gamma(0) = ?$$
 $\left(\int_{7}^{W} = 0\right)$

$$= \sum_{L} = (0; 0, 0, 1)$$

 ψ

must vanish for both theta=0 and theta=pi by the same helicity arguments as before for transverse W

$$\frac{d\Gamma(0)}{d-2} = \frac{g^2 M_W}{16\pi^2} \cdot \frac{1}{8} \sin^2 \theta \leftarrow \frac{NO P \text{ wildin!}}{(Wy???)}$$

answer: no preferred direction

$$\Gamma(0) = \frac{g^{-}H_{W} \cdot 2\pi}{16\pi^{-} \cdot 8} \int_{0}^{\pi} finodo fino \frac{1}{9/3}$$

$$\Gamma(0) = \frac{\int^{\infty} Hw}{48\pi} = \Gamma(+1) = \Gamma(-1)$$

must be same = rotational symmetry still present when W at rest

Excercise

hre:
$$\sum_{i} \epsilon_{\mu}^{(i)} \epsilon_{\nu}^{*(i)} = \left[-J_{\mu\nu} + \frac{J_{\mu}J_{\nu}}{M_{\mu\nu}^{2}} \right]$$

and he reed:

$$\sum \frac{1}{3} |M|^{2} = \frac{g^{2}}{12} T_{V} \left[-\frac{1}{3} \frac{1}{4} \frac{1}{4}$$

$$\Gamma_{W} = \frac{1}{4\pi^{2}} \frac{g^{2} H_{W}^{2}}{3} \int \frac{d^{2}p}{2po} \int \frac{d^{2}e}{2eo} \frac{1}{2H_{W}} \int_{0}^{(6)} (p+4-e)$$

$$T_{W} = \frac{1}{3} \left[\Gamma(+1) + \Gamma(-1) + \Gamma(0) \right]$$
ell equal = $\frac{9^{4} \text{ Hiv}}{48\pi}$

$$T_{W} = \frac{\alpha H_{W}}{120 \text{ shi } \Phi_{W}}$$

Obviously, must be the same, since all polarisations give the same

Total W decay

$$T(w \rightarrow e \bar{v}) = \frac{\angle Mw}{12 8 in^2 9w} \times \frac{13}{3} / 3 \text{ generatus}$$
of leptor

$$T(w \to ud) = \frac{\alpha Mw}{12 a \ln^2 b w} \times 3 (color) (mu = md = 0)$$

$$\int \int w = \frac{d Mw}{12 h'n'ow} \left(3+6\right) = \frac{3}{4} \frac{d Mw}{h'n'ow}$$

$$\Rightarrow T(w) \simeq \frac{Mw}{40} \simeq 2 \text{ GeV}$$

$$PD6: 2.085 \pm 0.042$$
There approximations we took

The uptern to equivalent to fermions way clay
$$t - axis$$
 and $t + b$ and $t +$

[Notes by Peshin , page 7) ucp) = Vzp 31 = Vzp (0) - femm (4 = -1/2) so ne centule: u(e) = 1.52 32 = 129 (d) - outr-femmen (h=+1/2) => W = 8/2 n+(p) on n(e) €µ = $=g\sqrt{2p\varrho} \otimes (01) \begin{bmatrix} \sin\theta & (1+\cos\theta) \\ (\cos\theta-1) & -\sin\theta \end{bmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix} \sqrt{2}$ p=e= g /2 p (cno-1) = -g p (1-ano) = -g Hw (1-ano) MW/2 notice: M=0, a 0 >0 as expected and cupated by Trace techniques = / M/2 = 9 Hw (1-cno)2 Formule (20) in my notes an Tw decay -no effort - only some Haglit · Sz=-1 = numediately topo i -- i => | M+ (-11 = 2 (1+ano)2

· lugihdul

$$\vec{\xi}_{L} = \begin{pmatrix} \alpha_{0} & 0 & -n'_{11} & 0 \\ 0 & 1 & 0 & 0 \\ n'_{10} & 0 & \alpha_{0} & 0 \end{pmatrix} = \begin{pmatrix} -n'_{11} & 0 \\ 0 \\ \alpha_{1} & 0 \end{pmatrix}$$

$$W(L) = \frac{g}{\sqrt{2}} \cdot 2p \left(01\right) \begin{bmatrix} cn\theta & -hn\theta \\ -Hn\theta & -cn\theta \end{bmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

pope 12 of my notes on w decey

one can of course heep W-splu on t-axis

and notate the spinors (or solve to h = -1/2 spinors Mu D

direction)

2(e)

$$M = \sqrt{25} \left(-\frac{\sin \theta h}{\cos \theta h} \right)$$

$$v = \sqrt{2E} \begin{pmatrix} \cos \theta/2 \\ \sin \theta/2 \end{pmatrix}$$

$$\Rightarrow |M|^2 = g^2 \frac{Mw^2}{4} (1 - cno)^2 V$$