


Domain walls

$$\bullet RT = \text{const} = 10^{30}$$

$$ds^2 = R^2(t) dx^2$$

$$H = \dot{R}/R = \frac{1}{t}$$

$$\pi = 4 = 1$$

$$\underbrace{R^3 T^3}_{\text{entropy}} = 10^{90}$$

$$n(\text{density}) = T^3 \quad (T \gg m)$$

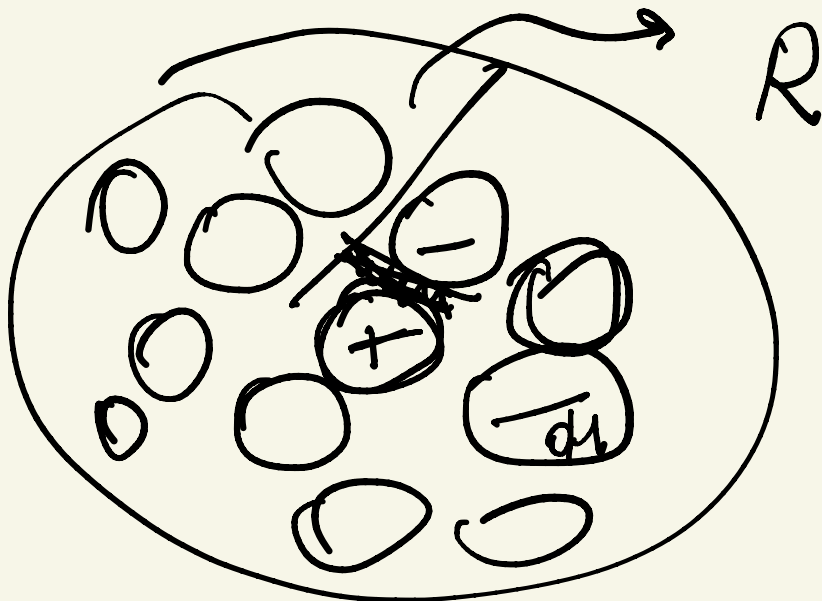
$$V = R^3$$

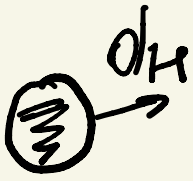
$$\boxed{R^3 T^3 = N} = \text{entropy}$$

- $R = \frac{10^{20}}{T} = \underline{\underline{\text{scale of universe}}}$

- $dH = t = \frac{1}{T} \cdot \left(\frac{M_{pl}}{T} \right)$

$$R(t) / dH(t) \gg 1 \quad T \gg u_e$$





→ exponential growth
(inflation)

Symmetries at high T

Dvali, G.S.

Is there a domain wall
therein?

Rochelle salt

Weinberg '79

High T

Gravity and Einstein well

$$R_{\mu\nu} - \frac{1}{2} g_{\mu\nu} R = -8\pi G T_{\mu\nu}$$

⇓

$$R_{\mu\nu} = -8\pi G \left(T_{\mu\nu} - \frac{1}{2} g_{\mu\nu} T \right)$$

⇓

$$T \equiv T^{\mu}_{\mu}$$

$$g_{\mu\nu} = \underset{\substack{\uparrow \\ \text{Lorentz metric}}}{\eta_{\mu\nu}} + h_{\mu\nu} \quad \text{field}$$

$$\eta_{\mu\nu} = \text{diag}(1, -1, -1, -1)$$

$$h_{00} = 2\phi$$

$$\square \phi \approx \left(T_{00} - \frac{1}{2} \gamma_{00} T \right)$$

Newton: $T_{00} = \rho$

$\rho > 0 \Leftrightarrow$ gravity =
attractive

$$T_{00} = \rho, \quad T_{ii} = p_i$$

with $p_i = 0$

domain wall (static)

$$T_{\mu\nu} = -\mathcal{L} g_{\mu\nu} + \partial_\mu \phi \frac{\partial \mathcal{L}}{\partial (\partial_\nu \phi)}$$

translations

[conserved energy -
momentum]

$$\mathcal{L} = \frac{1}{2} \partial_\mu \phi \partial^\mu \phi - V(\phi)$$

\Downarrow

$$T_{\mu\nu} = -\mathcal{L} \eta_{\mu\nu} + \partial_\mu \phi \partial_\nu \phi$$

\nearrow
 $\phi_{\text{wall}}(z)$

(x-y) plane

$$T_{00} = -\mathcal{L} + (\partial_0 \phi)^2 = -\mathcal{L}$$

$$T_{11} = +\mathcal{L} + (\partial_x \phi)^2 = +\mathcal{L}$$

$$T_{22} = +\mathcal{L} + (\partial_y \phi)^2 = +\mathcal{L}$$

$$T_{33} = \mathcal{L} + (\partial_z \phi)^2 =$$

$$= \underbrace{\frac{1}{2} \left(\frac{d\phi_w}{dz} \right)^2 - V}_{\text{well solution}} = 0$$

well solution

$$T_{00} = \frac{1}{2} \left(\frac{d\phi_w}{dt} \right)^2 + \bar{V} = 2\bar{V} \\ \equiv \rho$$

$$T_{11} = T_{22} = -\rho$$

$$\nabla^2 \phi \propto (T_{00} - \frac{1}{2} T)$$

$$T = T_0 + T_1 + T_2 + T_3$$

$$= \rho + \rho + \rho = 3\rho$$

$$T_1 = -T_{11}$$

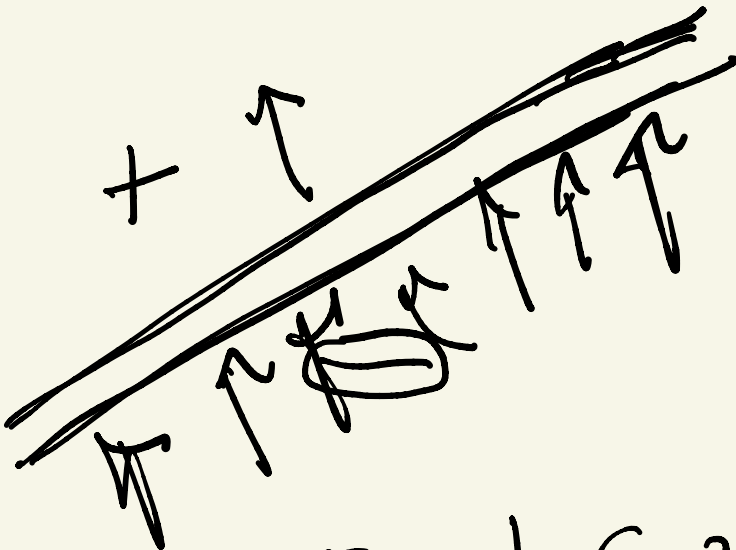
$$T_2 = -T_{22}$$



$$\nabla^2 \phi \propto (\rho - \frac{1}{2} 3\rho)$$

$$= -\rho$$

"anti-gravity"



Rai, G.S.
1994

$$V = \frac{1}{4} (\phi^2 - v^2)^2 + \frac{\phi^5}{M_{pl}^5}$$

$\in v^3 \phi$

$\phi \approx v$



$$E \approx 10^4$$

$$\longleftrightarrow \frac{10^5}{M_{pl}}$$

$$\Sigma \approx \frac{10^4}{M_{pl}}$$

$$V = 1 \text{ TeV} = 10^3 \text{ GeV}$$

$$10^{-15}$$

$$\begin{array}{l} G_{\text{N}} \rightarrow 0 \\ M \rightarrow \infty \end{array}$$

Handwriting

$$R_s = G_{\text{N}} M = \text{finite}$$

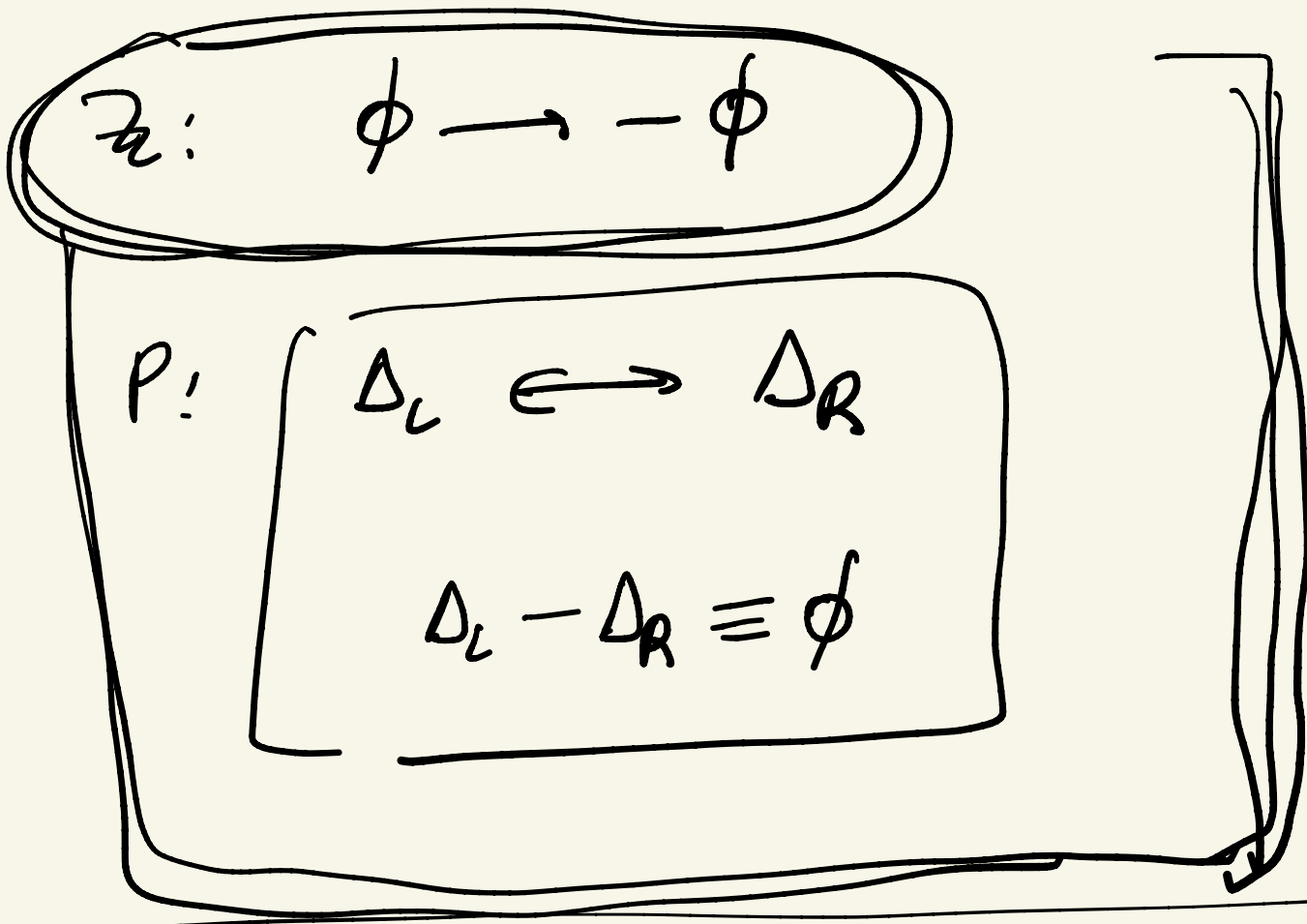
N (gravitons)

$$\Leftrightarrow N \rightarrow \infty$$

$$\frac{1}{N}$$

$$\Sigma = 10^{-30}$$

curly



$CP:$

$$\psi_L \xrightarrow{P} \psi_R$$

$$\psi_L \xrightarrow{C} C \bar{\psi}_R^T$$

$$\Rightarrow \psi_L \rightarrow C \bar{\psi}_L^T$$



SM: ~~P, C~~ maximally broken

$W_\mu \gamma_L^\mu$ (NO RH)

CP Spont.?

T.D. Lee
'73

(X) $W_\mu^+ \bar{u}_L \gamma^\mu d_L + x^* W_\mu^- \bar{d}_L \gamma^\mu u_L$

$CP \rightarrow x \bar{d}_L \gamma^\mu u_L W_\mu^-$

$CP \iff x = x^*$

$x \in C$ du SM?

$$-M_\nu = U_{L\nu}^+ M_\nu U_{R\nu}$$

$$V_{CKM} = U_{LU}^\dagger U_{LD} \in \mathbb{C}$$

$$\Leftrightarrow \text{CP}$$

$$\Leftrightarrow M_e \in \mathbb{C}$$

$$M_e = Y_e \langle \Phi \rangle \in \mathbb{C}$$

~~CP~~ \Rightarrow real before SM breaking

$$\Rightarrow Y_e \in \mathbb{R}$$

Can I break CP spont.
in SM?

$\Leftrightarrow \langle \phi \rangle \in \mathbb{C} ??$

Qto: $\langle \phi \rangle = \text{real} ?$

$$\langle \Phi \rangle = \Phi_0 = \begin{pmatrix} 0 \\ v e^{i\alpha} \end{pmatrix} \equiv \overline{\Phi}_0^c$$

Qto: $\alpha = 0 ?$

Yes $\Phi_0^c = \underbrace{e^{-i\alpha}}_{v(i)} \overline{\Phi}_0^c = \begin{pmatrix} 0 \\ v \end{pmatrix}$

"Minimal" extension of SM:
spont. $\mathbb{C}P$

we like $\bar{\Phi} = \text{doublet}(s)$

$$\Rightarrow \rho = \frac{M_Z \cos \theta}{M_W} = 1$$

$\Phi_1, \Phi_2 \leftarrow T, D. \text{lee}$

$$\langle \Phi_1 \rangle = \begin{pmatrix} 0 \\ v_1 \end{pmatrix} \quad \langle \Phi_2 \rangle = \frac{v}{2} \begin{pmatrix} \cos \theta e^{i\alpha} \\ \sin \theta e^{i\beta} \end{pmatrix}$$

$$Q_{em} \langle \Phi_i \rangle = 0$$

\Downarrow

$$\langle \Phi_2 \rangle = \frac{v}{2} \begin{pmatrix} 0 \\ e^{i\beta} \end{pmatrix}$$

$$\propto (\Phi_1^\dagger \Phi_2)(\Phi_2^\dagger \Phi_1)$$

$$\Rightarrow \propto v_1^2 v_2^2 \sin^2 \theta$$

$$\underline{\alpha < 0} \Rightarrow \boxed{\sin \theta = 1}$$

$$\langle \Phi_2 \rangle = \begin{pmatrix} 0 \\ \frac{1}{2} e^{i\delta} \end{pmatrix} \quad \text{CP phase}$$



$$\rightarrow \phi_1^\dagger \phi_1 (\phi_1^\dagger \phi_2 + \text{h.c.})$$
$$\rightarrow (\phi_1^\dagger \phi_2)^2 + \text{h.c.}$$

$$\boxed{V = A \cos \delta + B \cos 2\delta + C}$$

$$\boxed{A, B \neq 0 \therefore \delta \neq 0}$$

$$M_Z = Y_e^1 \langle \phi_1 \rangle + Y_e^2 \langle \phi_2 \rangle$$

a mess!

SM and phase transition

$$T_c \approx M_W \approx 100 \text{ GeV}$$

$$1 \text{ eV} \approx 10^4 \text{ K}$$

$$T_c \approx 10^{15} \text{ K}$$

Generations

Why generations?

mass: who ordered that?

$$m_i \neq m_j \quad (\Leftrightarrow \nabla_{ij})$$

high energy \Leftrightarrow mass irrelevant

Family = generations

Family by unity?

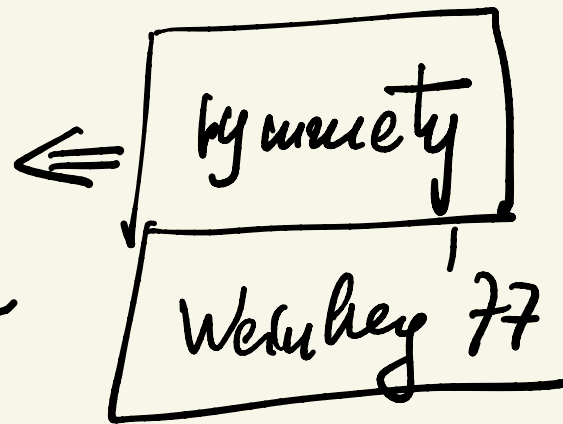
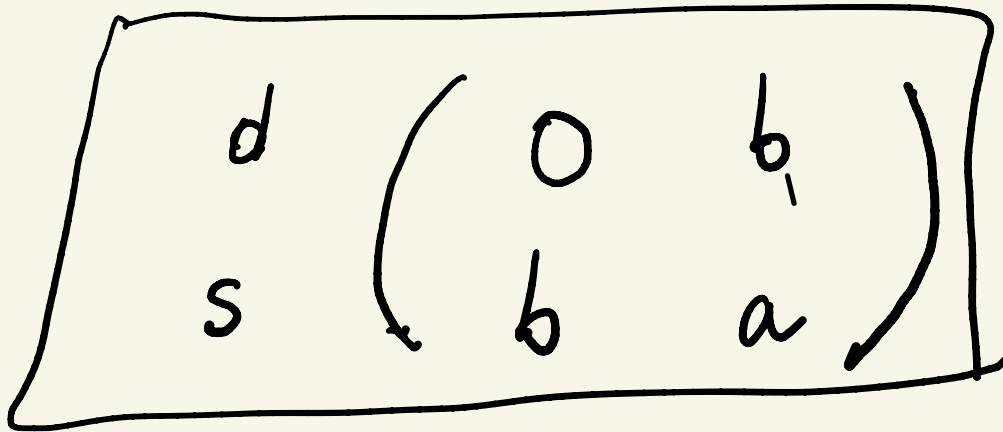
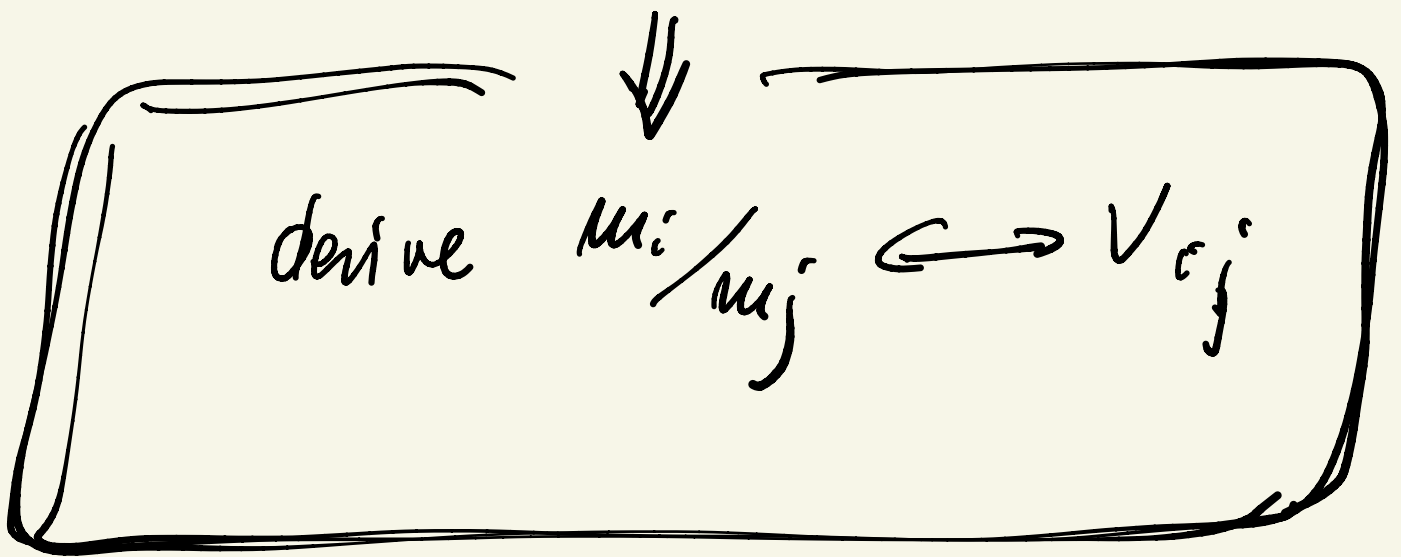
$SO(3)$

\rightarrow

$SU(3)$

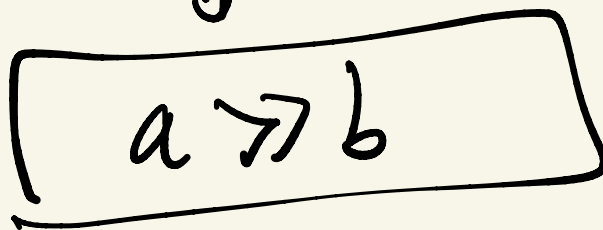
\downarrow split

$\mathbb{1}$



$$M_2 = U_L^+ m_q U_R$$

$m_s \gg m_d$ ($m_s \approx 100 \text{ MeV}$,
 $m_d \approx 5 \text{ MeV}$)



$$u_s \approx a, \quad u_d \approx b^2/a$$

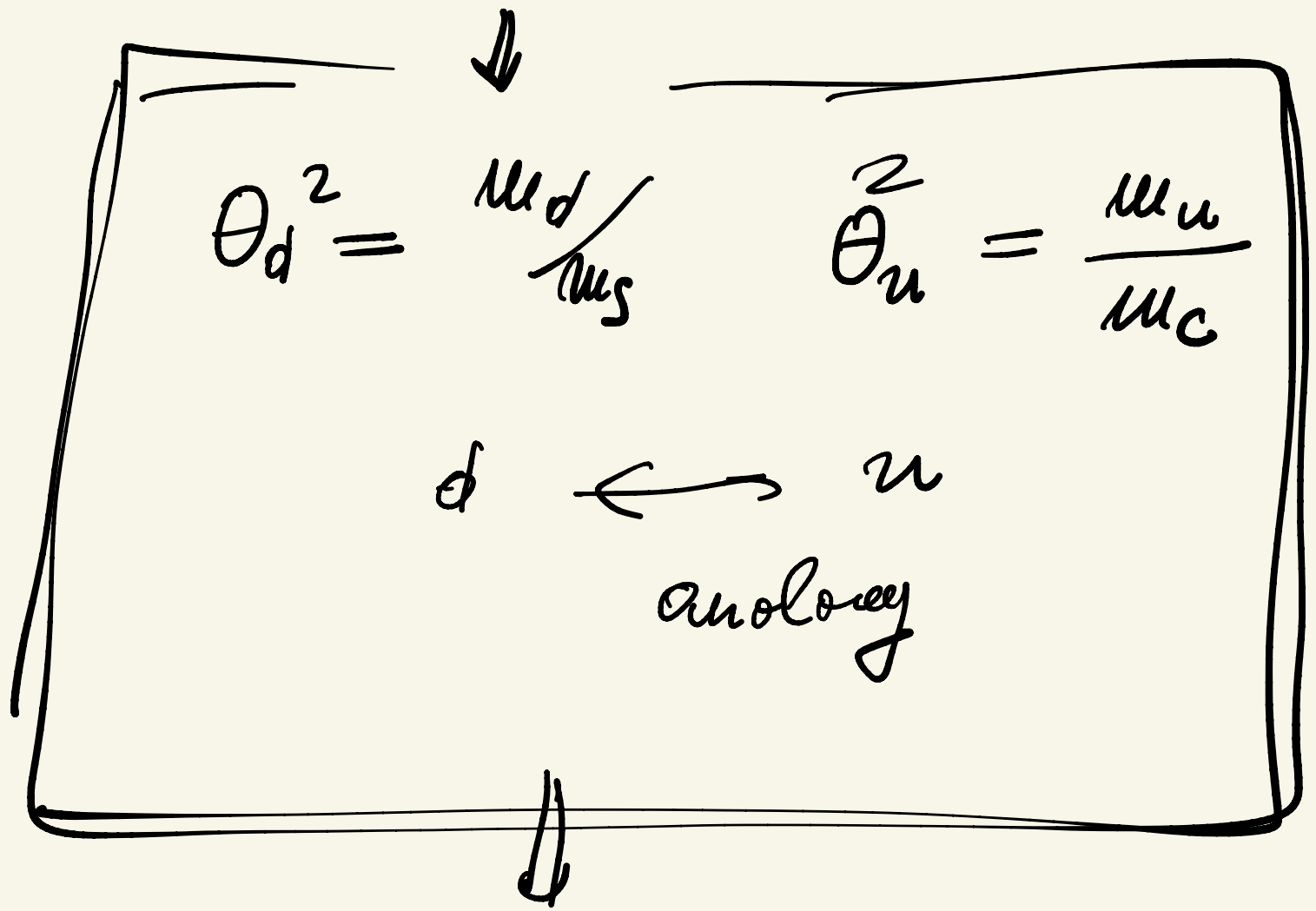
$$\frac{1}{2} \tan 2\theta = \frac{b-c}{a}$$

$$\begin{pmatrix} c & b \\ b & a \end{pmatrix} = O(\theta) \begin{pmatrix} u_1 & 0 \\ 0 & u_2 \end{pmatrix} O^T(\theta)$$

$$O(\theta) = \begin{pmatrix} c & s \\ -s & c \end{pmatrix}$$

$$\Rightarrow \theta \approx b/a$$

$$\theta^2 \approx b^2/a^2 = u_d/u_s$$



$$V_{cd} = V_{cu}^\dagger U_{cd}$$

$$\theta_c = \theta_d - \theta_u = \sqrt{\frac{m_d}{m_s}} - \sqrt{\frac{m_u}{m_c}}$$

$$\Rightarrow \theta_c^2 \approx \frac{m_d}{m_s}$$

in practice

Nice symmetry \Rightarrow nice relations

m_u	m_c	m_t	$\bar{V}_{cu} = 1$
m_d	m_s	m_b	

\Rightarrow BSM Heavy

$$W (\theta_c = \theta_d - \theta_u)$$

$$\uparrow \quad \uparrow$$
 GUT: $\bar{X} \quad \theta_u \quad ; \quad \theta_d$

$$\theta_2 \approx 0 \quad \left(\begin{array}{l} \theta_c \approx 13^\circ \\ (12) \end{array} \right), \quad \theta_{23} \approx 10^\circ, \\ \theta_{13} \approx 10^{-3}$$

$$\theta_e \approx (30^\circ, 45^\circ, 10^\circ)$$

Why not unity int. + fermions?



$SO(10)$: 1 family

$SO(18)$ \Leftarrow 3 family

G.S, Wilczek, Feb
'84

Minimal $SU(5)$

GG



wrong!